

Calcolo di Limiti

Calcolare i seguenti limiti:

$$1. \lim_{x \rightarrow 1} \frac{2x-1}{\log x - 3} = \left(-\frac{1}{3}\right)$$

$$2. \lim_{x \rightarrow +\infty} \frac{3x^2 - 2x + 1 + x^5}{3x^2 + 4x - 1} = (+\infty)$$

$$3. \lim_{x \rightarrow -\infty} \frac{2x^5 - x^3 + x^4}{x^5 - 6x^2} = (2)$$

$$4. \lim_{x \rightarrow +\infty} \frac{\sqrt{4x^2 - 3}}{x + 1} = (2)$$

$$5. \lim_{x \rightarrow 3} \frac{x^2 - 3x}{x^2 - 9} = \left(\frac{1}{2}\right)$$

$$6. \lim_{x \rightarrow 5^+} \frac{1-2x}{x-5} = (-\infty)$$

$$7. \lim_{x \rightarrow +\infty} \left(1 - \frac{1}{\log x}\right) = (1)$$

$$8. \lim_{x \rightarrow 0^+} \left(1 - \frac{1}{\log x}\right) = (1)$$

$$9. \lim_{x \rightarrow 1^-} \left(1 - \frac{1}{\log x}\right) = (+\infty)$$

$$10. \lim_{x \rightarrow 1^+} \left(1 - \frac{1}{\log x}\right) = (-\infty)$$

$$11. \lim_{x \rightarrow +\infty} \left(2^x + \frac{3}{x}\right) = (+\infty)$$

$$12. \lim_{n \rightarrow +\infty} (e^n - 2n) = (+\infty)$$

$$13. \lim_{x \rightarrow +\infty} \sqrt{x} \ln x = (+\infty)$$

$$14. \lim_{n \rightarrow +\infty} \frac{2^{-n}}{5n} = (+\infty)$$

$$15. \lim_{n \rightarrow +\infty} (e^{-n} - 2n) = (-\infty)$$

$$16. \lim_{x \rightarrow +\infty} \left(\frac{1 - \ln x}{e^{-x}}\right) = (-\infty)$$

$$17. \lim_{n \rightarrow +\infty} \left(\left(\frac{1}{2}\right)^n \cdot 3^n\right) = (+\infty)$$

$$18. \lim_{x \rightarrow +\infty} (x^2 - 2x) = (+\infty)$$

$$19. \lim_{x \rightarrow -\infty} \frac{x^2}{x+5} = (-\infty)$$

$$20. \lim_{n \rightarrow +\infty} \frac{n+5}{n^2} = (0^+)$$

$$21. \lim_{x \rightarrow +\infty} \frac{x+2}{2x+1} = \left(\frac{1}{2}\right)$$

$$22. \lim_{x \rightarrow +\infty} \frac{3x^3 - 2x^2 + 10x}{x^3 + 1} = (3)$$

$$23. \lim_{n \rightarrow +\infty} \frac{n \ln n + 3}{e^{-n} - 8 \ln n} = (+\infty)$$

$$24. \lim_{n \rightarrow +\infty} \frac{-5n^3}{e^n} = (0^-)$$

$$25. \lim_{x \rightarrow +\infty} \frac{x \ln x}{2 \ln^5 x} = (+\infty)$$

$$26. \lim_{n \rightarrow +\infty} (4 \ln^3 n - \sqrt{n}) = (-\infty)$$

$$27. \lim_{x \rightarrow +\infty} \frac{2 \ln x - 3\sqrt{x}}{\sqrt[3]{x} + 5} = (+\infty)$$

$$28. \lim_{x \rightarrow +\infty} \frac{x^2 + 3}{2^x + 3x^2} = (0^+)$$

$$29. \lim_{n \rightarrow +\infty} \frac{n^2 + 3}{2^{-n} + 3n^2} = \left(\frac{1}{3}\right)$$

$$30. \lim_{x \rightarrow +\infty} \frac{1 + 0,1x}{1 + 0,15x} = \left(\frac{2}{3}\right)$$

$$31. \lim_{n \rightarrow +\infty} \frac{(1,001)^n}{n^{1000}} = (+\infty)$$

$$32. \lim_{n \rightarrow +\infty} \frac{1000^n}{n!} = (0)$$

$$33. \lim_{x \rightarrow 1^-} \frac{1}{x-1} = (-\infty)$$

$$34. \lim_{x \rightarrow 1^+} \frac{1}{x-1} = (+\infty)$$

$$35. \lim_{x \rightarrow 1^-} \frac{x-2}{(x-1)^2} = (-\infty)$$

$$36. \lim_{x \rightarrow 1^+} \frac{x-2}{(x-1)^2} = (-\infty)$$

$$37. \lim_{x \rightarrow 0^-} \frac{\ln x}{e^x - 1} = (+\infty)$$

38. $\lim_{x \rightarrow 0^+} \frac{x^2 - 3x}{\ln x + 4} = (0^-)$
39. $\lim_{x \rightarrow 2^-} \frac{x^2 - 4}{x^2 - 4x + 4} = (-\infty)$
40. $\lim_{x \rightarrow +\infty} (\ln x + e^{-x} + x^{-3}) = (+\infty)$
41. $\lim_{x \rightarrow +\infty} \frac{\sqrt[7]{x^3} + 3}{\sqrt{x} - 2} = (0)$
42. $\lim_{x \rightarrow 0^+} \frac{x^{-3} + 3^x}{\frac{1}{x^2}} = (+\infty)$
43. $\lim_{x \rightarrow \frac{1}{2}^-} \frac{\ln x}{1 - 2x} = (-\infty)$
44. $\lim_{x \rightarrow \frac{1}{2}^+} \frac{\ln x}{1 - 2x} = (+\infty)$
45. $\lim_{x \rightarrow 2^-} \frac{e^x - 8}{4 - 4x + x^2} = (-\infty)$
46. $\lim_{x \rightarrow 2^+} \frac{e^x - 8}{4 - 4x + x^2} = (-\infty)$
47. $\lim_{n \rightarrow +\infty} \frac{2n^3 - 5 - n(\ln(n^2))^4}{100n + 3n^2} = (+\infty)$
48. $\lim_{x \rightarrow +\infty} \frac{2^{-x}}{x^2 + 3} = (0)$
49. $\lim_{n \rightarrow +\infty} \left(1 + \frac{2}{n}\right)^n = (e^2)$
50. $\lim_{x \rightarrow +\infty} \frac{\ln x - \sqrt{x}}{2 - \sqrt[3]{x}} = (+\infty)$
51. $\lim_{x \rightarrow +\infty} \frac{x - \sqrt{x}}{x + \ln 3^x} = \left(\frac{1}{1 + \ln 3}\right)$
52. $\lim_{n \rightarrow +\infty} \frac{(n - \ln n)^2}{n^2 + n^{\frac{3}{2}} \ln n} = (1)$
53. $\lim_{n \rightarrow +\infty} \frac{2 - 3\sqrt{n}}{n^k + \sqrt{n}} \quad (k \in \mathbb{R}_+)$
54. $\lim_{n \rightarrow +\infty} \frac{\ln n - \sqrt{n^3}}{\sqrt[3]{n} + 5n^a} \quad (a \in \mathbb{R})$
55. $\lim_{n \rightarrow +\infty} \left(\frac{1+a}{3}\right)^n \quad (a \in \mathbb{R}_+)$
56. $\lim_{n \rightarrow +\infty} \frac{n^a - \ln n}{4\sqrt{n}} \quad (a \in \mathbb{R}_+)$
57. $\lim_{n \rightarrow +\infty} \frac{kn^3 - n^2 + \sqrt{n}}{2n^2(k^2 + 3) + 5} \quad (k \in \mathbb{R})$
58. $\lim_{n \rightarrow +\infty} \frac{\sqrt{n}}{(n+2)n^a} \quad (a \in \mathbb{R})$
59. $\lim_{n \rightarrow +\infty} \frac{a^n + 2^n}{3^n} \quad (a \in \mathbb{R}_+)$