### International Financial and Foreign Exchange Markets

#### letting Started

I/B Decisions and Currencies of Denomination

overed Interes ate Parity

Definition
Deviations and
Arbitrage
Opportunities
Building Synthetic

erminolog

To Put It in Practice

# Lesson III: The Relationship among Spot, Fwd and Money Mkt Rates

Monday 12<sup>th</sup> March, 2018



## Table of Contents

International Financial and Foreign Exchange Markets

**Getting Started** 

I/B Decisions and Currencies of Denomination

Covered Interest Rate Parity

Definition
Deviations and Arbitrage Opportunities
Building Synthetic Securities

**Terminology** 

To Put It into Practice

Getting Started

I/B Decisions and Currencies of Denomination

overed Interest ate Parity

Definition
Deviations and
Arbitrage
Opportunities
Building Synthetic
Securities

erminology

To Put It in Practice

### **Getting Started**

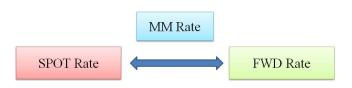
I/B Decisions and Currencies of Denomination

Covered Interest Rate Parity

Definition
Deviations and
Arbitrage
Opportunities
Building Synthetic

Termino

Fo Put It int Practice



## Investing on an International Scale

Assume you have some funds to place in the money market for 3 months: how to choose between **domestic and foreign currency-denominated** securities?



International Financial and Foreign Exchange Markets

Getting Started

### I/B Decisions and Currencies of Denomination

Covered Interest Rate Parity

Definition
Deviations and
Arbitrage
Opportunities
Building Synthetic

erminology

To Put It into Practice

Getting Started

I/B Decisions and Currencies of Denomination

Covered Interest Rate Parity

Definition
Deviations and
Arbitrage
Opportunities
Building Synthetic

erminology

To Put It into Practice

Relying **exclusively** on interest rate differentials might be seriously misleading: **both** interest and exchange rates should be taken into due account

Getting Started

### I/B Decisions and Currencies of Denomination

Covered Interest Rate Parity

Definition
Deviations and
Arbitrage
Opportunities
Building Synthetic

erminology

To Put It int Practice

If you decide to invest in a USD-denominated security (assuming the USD is the domestic currency), at the end of the investment period you would get

$$1+rac{r_{USD}}{4}$$



If you conversely decide to invest in a foreign-currency denominated security (assume GBP), you would have to:

▶ **Buy GBP**, thus getting

$$\frac{1}{S_{USD}}$$

► Invest the amount above in a GBP-denominated asset and get (at maturity)

$$\frac{1}{S_{\frac{USD}{GBP}}} \cdot \left(1 + \frac{r_{GBP}}{4}\right)$$

Sell GBP forward in order to receive

$$\frac{F_{0.25\frac{USD}{GBP}}}{S_{\frac{USD}{GBP}}} \cdot \left(1 + \frac{r_{GBP}}{4}\right)$$

Getting Started

I/B Decisions and Currencies of Denomination

Rate Parity
Definition
Deviations and
Arbitrage
Opportunities
Building Synthetic

erminolog

To Put It in Practice

I/B Decisions and Currencies of Denomination

You will be indifferent between the two options only if

$$1 + \frac{r_{USD}}{4} = \frac{F_{0.25 \frac{USD}{GBP}}}{S_{USD}} \cdot \left(1 + \frac{r_{GBP}}{4}\right)$$



$$r_{USD} = r_{GBP} + 4 \cdot \frac{F_{0.25} \frac{USD}{GBP} - S_{USD}}{S_{USD}}$$

With

- ► Annualised GBP interest rate: r<sub>GBP</sub>
- ► Annualised fwd premium/discount on GBP:

$$4 \cdot \frac{F_{0.25} \frac{USD}{GBP} - S_{USD}}{S_{USD}}$$



Getting Started

I/B Decisions and Currencies of Denomination

Definition
Deviations and
Arbitrage

Deviations and Arbitrage Opportunities Building Synthetic Securities

erminology

To Put It in Practice

$$(1+r_D)^n = \frac{F_{n\frac{D}{F}}}{S_{\frac{D}{F}}} (1+r_F)^n$$



Setting Started

International

Financial and Foreign Exchange Markets

/B Decisions and Currencies of Denomination

Covered Interest Rate Parity

### Definition

Deviations and Arbitrage Opportunities Building Synthetic Securities

erminology

To Put It int Practice



Getting Started

I/B Decisions and Currencies of Denomination

Covered Interest
Rate Parity

### Definition

Deviations and Arbitrage Opportunities Building Syntheti

erminology

To Put It into Practice

When steps have been taken to avoid foreign exchange risk by use of forward contracts (hence the term "covered"), rates of return on investments and costs of borrowing will be equal, irrespective of the currency of denomination (ceteris paribus)



## Lifting the Curtain on the Ceteris Paribus Condition

There must be **no** frictions for the CIRP to hold perfectly, meaning **no** legal restrictions on the movement of K, **no** tax advantages among different countries...



International Financial and Foreign Exchange Markets

etting Started

I/B Decisions and Currencies of Denomination

Covered Interest
Rate Parity

## Definition Deviations a

Deviations and Arbitrage Opportunities Building Synthetic Securities

erminology

To Put It into Practice Suppose that

$$(1+r_D)^n < \frac{F_{n\frac{D}{F}}}{S_{\frac{D}{F}}}(1+r_F)^n$$

The best thing to do would be **to borrow in your domestic currency** and **to invest simultaneously in a foreign currency-denominated security**. At the end of the investment period, the hedged transaction will allow you to get more than required to repay the initial debt (i.e. you will receive more domestic currency)



etting Started

/B Decisions and Currencies of Denomination

overed Interest ate Parity

Deviations and Arbitrage Opportunities Building Synthetic

ecurities

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To Put It in Practice L/P Designed

 $(1+r_D)^n > \frac{F_{n\frac{D}{F}}}{S_{\frac{D}{F}}}(1+r_F)^n$ 

The best thing to do would be **to borrow foreign currency** and **to invest simultaneously in a domestic currency-denominated security**. At the end of the investment period, the hedged transaction will allow you to get more than required to repay the initial debt



If, conversely,

etting Started

/B Decisions and Currencies of Denomination

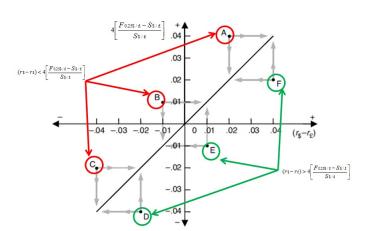
Rate Parity

Deviations and Arbitrage Opportunities

Opportunities
Suilding Synthetic
ecurities

erminology

To Put It in



International Financial and Foreign Exchange Markets

etting Started

I/B Decisions and Currencies of Denomination

overed Interest ate Parity

Deviations and Arbitrage Opportunities

Spportunities

Building Synthetic

Becurities

Terminology

To Put It in

For all the **points lying above the equilibrium line** (A,B) and C), it must be that

$$(r_{USD} - r_{GBP}) < 4 \cdot \frac{F_{n \frac{USD}{GBP}} - S_{\frac{USD}{GBP}}}{S_{\frac{USD}{GBP}}}$$

This further implies:

- Covered investment in GBP yields more than in USD
- Borrowing in USD is cheaper than covered borrowing in GBP

Deviations and

Arbitrage Opportunities



- 1. **Borrow USD**, thus tending to increase  $r_{USD}$
- 2. Buy spot GBP with the borrowed USD, thus tending to increase  $S_{\frac{USD}{CBP}}$
- Buy a GBP-denominated security, thus tending to reduce r<sub>GBP</sub>
- 4. Sell the GBP investment proceeds forward for USD, thus tending to reduce  $F_{0.25\frac{USD}{GRP}}$

Points 1 to 4 will all push A, B and C back down to the CIRP line

Getting Started

Currencies of Denomination

Rate Parity
Definition
Deviations and

Arbitrage
Opportunities
Building Synthetic

minology

erminology

To Put It int Practice For all the **points lying below the equilibrium line** (D, E and F), it must be that

$$(r_{USD} - r_{GBP}) > 4 \cdot \frac{F_{n \frac{USD}{GBP}} - S_{\frac{USD}{GBP}}}{S_{\frac{USD}{GBP}}}$$

This further implies:

- Covered investment in USD yields more than in GBP
- Borrowing in GBP is cheaper than covered borrowing in USD

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/B Decisions and Currencies of Denomination

overed Interest ate Parity

Deviations and Arbitrage Opportunities Building Synthetic

Building Synthetic lecurities

erminology

To Put It into Practice

- 1. **Borrow GBP**, thus tending to increase  $r_{GBP}$
- 2. **Buy spot USD** with the borrowed GBP, thus tending to decrease  $S_{\frac{USD}{CDD}}$
- Buy a USD-denominated security, thus tending to reduce r<sub>USD</sub>
- 4. **Sell the USD investment proceeds forward** for GBP, thus tending to increase  $F_{0.25\frac{USD}{CBP}}$

Points 1 to 4 will all push D, E and F back up to the CIRP line

etting Started

Currencies of
Denomination

Rate Parity
Definition
Deviations and

Arbitrage Opportunities Building Synthetic

erminology

To Put It into Practice

## **Empirical Findings**

Persistent deviations from the CIRP are **unlikely** to occur, because this would give rise to arbitrage opportunities (**No Free Lunch Principle**)



International Financial and Foreign Exchange Markets

Getting Started

I/B Decisions and Currencies of Denomination

Covered Interest

Definition

Deviations and

Arbitrage
Opportunities
Building Synthetic

erminology

To Put It into

Covered investment/borrowing involve **two FX transactions** (one on the spot market and the other on the forward market).

Transaction costs have to be faced twice.

One may be lead to think there **could be deviations** from interest rate parity due to the **extra transaction costs** of investing/borrowing in foreign currency...

Is it always and necessarily so?



Setting Started

/B Decisions and Currencies of Denomination

Covered Interest Cate Parity

Deviations and Arbitrage Opportunities

Building Synthetic ecurities

erminology

To Put It int Practice

## Case 1: Round-Trip Transactions

vielding GBP, after n-months...

STEP 4: GBP<sub>n</sub> are sold at the STEP 1: Suppose that, at time 0, STEP 1: forward rate F(\$/bid£) stipulated vou borrow USD<sub>0</sub> Assume Borrow at time 0, thus obtaining USD, further that the interest rate on (USD required to repay the debt) such borrowing is r<sub>BUSD</sub> STEP 4: STEP 2: STEP 3: the GBP amount STEP 2: the borrowed USD are STEP 3: obtained after Step 2 is placed in exchanged into GBP at S(\$/ask£) Invest in GBP-denominated deposit GBP

International Financial and Foreign Exchange Markets

Getting Started

I/B Decisions and Currencies of Denomination

overed Interest

Definit

Deviations and Arbitrage Opportunities Building Synthetic

Terminology

To Put It int Practice

$$(1 + r_{BUSD})^n = \frac{F_{n \underbrace{USD}_{bidGBP}}}{S\underbrace{USD}_{askGBP}} \cdot (1 + r_{IGBP})^n$$

This is **NOT** a perfect equilibrium line on the CIRP diagram, but more a "band" drawn around mid-rates. This is because of the transactions costs to be faced:

- ▶ Bid/Ask spread:  $S_{\frac{USD}{askGBP}} F_{n\frac{USD}{bidGBP}}$
- ► Borrowing/Investment spread:(r<sub>BUSD</sub> r<sub>IGBP</sub>)

Getting Started

/B Decisions and Currencies of Denomination

Definition
Deviations and
Arbitrage
Opportunities
Building Synthetic

erminology

To Put It into Practice If you need  $GBP_n$  sometime in the future and you have  $USD_0$  today, you could:

- ▶ Alternative 1: invest the USD you have in USD-denominated security and use the proceeds of the foregoing investment to buy GBP fwd (when they are needed)
- ► Alternative 2: sell the USD you have to buy GBP and invest them in a GBP-denominated security, yielding the GBP amount you need at maturity



Getting Started

I/B Decisions and Currencies of Denomination

Covered Interest Rate Parity

Deviations and Arbitrage Opportunities

uilding Syntheti ecurities

Ferminology

To Put It int

## Case 2: One-Way Transactions II

STEP 1: invest USD<sub>0</sub> in a USD-STEP 2: Use the proceeds (USD<sub>n</sub>) to denominated deposit buy GBP forward at Fn(\$/ask£), when GBP are needed. **STEP 2**: Use the proceeds to STEP 1: Invest in USD buy GBP fwd STEP 2: invest the GBP in a GBP-STEP 1: sell USD for GBP on denominated deposit yielding GBP, the spot mkt at S(\$/ask£) when GBP are needed. STEP 1: Sell USD to buy GBP

International Financial and Foreign Exchange Markets

Getting Started

I/B Decisions and Currencies of Denomination

overed Interest ate Parity

Deviations and Arbitrage Opportunities

erminology

To Put It into Practice

Getting Started

I/B Decisions and Currencies of Denomination

Lovered Interest Rate Parity Definition

Deviations and Arbitrage Opportunities Building Synthetic

ecurities

erminology

To Put It int Practice

Based on the CIRP,

$$(1 + r_{IUSD})^n = \frac{F_{n \text{ USD}}}{S \text{ USD} \atop S \text{ USD}} (1 + r_{IGBP})^n$$

This would plot an **exact** line in the CIRP diagram, given that there are virtually **no** transaction costs:

- ▶ Bid/Ask spread:  $S_{\frac{USD}{askGBP}} F_{n\frac{USD}{askGBP}}$
- **Borrowing/Investment spread**:  $(r_{IUSD} r_{IGBP})$

Getting Started

I/B Decisions and Currencies of Denomination

Rate Parity
Definition
Deviations and

Arbitrage Opportunities Building Synthetic

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Terminolog 4 6 1

To Put It into Practice

For round-trip arbitrages to be profitable, deviations from the CIRP line must be large enough to overcome transaction costs...and this will hardly ever occur in practice (Could you explain why?)

Transaction costs do **not** bring about profitable arbitrage opportunities



Covered Interest Rate Parity

Definition Deviations and Arbitrage

Building Synthetic Securities

erminology

To Put It in: Practice

## Rearranging the CIRP...

$$F_{n\frac{D}{F}} = S_{\frac{D}{F}} \cdot \frac{(1+r_D)^n}{(1+r_F)^n}$$



$$F_{n\frac{D}{F}}$$

...can be constructed by combining a spot contract

...with fixed-rate, n-period borrowing and lending in the domestic and foreign currencies respectively.

$$\frac{(1+r_D)^n}{(1+r_D)^n}$$

Getting Started

I/B Decisions and Currencies of Denomination

Rate Parity
Definition

Deviations and Arbitrage Dpportunities

Building Synthetic Securities

erminology

To Put It int

$$(1+r_D)^n=(1+r_F)^n\cdot\frac{F_{n\frac{D}{F}}}{S_{\frac{D}{F}}}$$

A synthetic domestic currency-denominated security

$$(1 + r_D)^n$$

... can be obtained by combining a foreign currency-denominated security

$$(1 + r_F)^n$$

...with a forward/spot swap

$$\frac{F_{n\frac{D}{F}}}{S_{\underline{D}}}$$

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**Building Synthetic** Securities



### The **CIRP** is useful:

- when trying to understand the direction of K movements (towards the currency with higher covered yield)
- ▶ to **build/replicate** a financial contract
- to hedge a financial position



### Getting Started

I/B Decisions and Currencies of Denomination

Covered Interest Rate Parity

Deviations and Arbitrage Opportunities

Building Synthetic Securities

Terminology

To Put It into

Currencies of Denomination

Rate Parity
Definition
Deviations and
Arbitrage
Opportunities
Building Synthetic

### Terminology

To Put It int Practice

**Synthetic Security**: financial instrument that is created artificially by combining the features of a collection of other assets



- ▶ Round-Trip Transaction: Borrowing in one currency, lending in another, and then selling the second currency back into the first so as to end up back in the first currency (*id est*, you start with a currency and you end up with the same one).
- ▶ One-Way Transaction: The process of choosing the best way to exchange one currency for another or choosing the best currency in which to invest or borrow (*id est*, you start with a currency and you end up with a different one).

Rate Parity
Definition
Deviations and
Arbitrage
Opportunities
Building Synthetic
Securities

## Terminology

To Put It into Practice



$\mathbf{S}_{rac{C_1}{C_2}}$	0.64
$ \mathbf{r}_{1y-C_1} $	0.05
$\mathbf{r}_{1y-C_2}$	0.09

- Calculate the theoretical price of a one year forward contract
- ▶ What would you do if the forward price was quoted at  $F_{1\frac{C_1}{C_2}}$ =0.65 in the market place? Where would you borrow? Lend? Calculate the gain on a C<sub>1</sub> 100 million arbitrage transaction
- ▶ What would you do if the forward price was quoted at  $F_{1\frac{C_1}{C_2}}$ =0.6 in the market place? Where would you borrow? Lend? Calculate the gain on a C<sub>2</sub> 100 million arbitrage transaction

International Financial and Foreign Exchange Markets

Getting Started

I/B Decisions and Currencies of Denomination

Rate Parity
Definition
Deviations and
Arbitrage
Opportunities
Building Synthetic
Securities

erminology

To Put It into Practice



**3.2**: The following exchange rates and one-year interest rates exist.

	Bid	Ask
$\mathbf{S}_{rac{A}{B}}$	1.52	1.63
$F_{1rac{A}{B}}^{^{B}}$	1.42	1.53

	Deposit	Loan
$r_A$	0.04	0.09
$\mathbf{r}_B$	0.05	0.1

You have 100 A to invest for 1 year. Would you benefit from engaging in covered interest arbitrage?



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etting Started

I/B Decisions and Currencies of Denomination

overed Interest ate Parity

Definition
Deviations and
Arbitrage
Opportunities
Building Synthetic

Terminology

To Put It into Practice