

# Outline

Case study 2 “Mechoff”

## **Design of manufacturing systems – Cellular Manufacturing**

- Top management’s questions
- Solution: objective, procedure, alternatives
- Concluding remarks

# MECHOFF – *Top Management's questions*



- Is it possible to meet the demand with **manufacturing cells**?

If yes, some questions to be answered may be:

- How many **machines** do I need?
- How many **fixtures** do I need?

# MECHOFF – Draft solution

## Objective

**To evaluate the alternative to switch from a job shop configuration to cellular manufacturing**

Assumptions:

- Products from the same family share the same fixture, built to take advantage of similar shapes:
  - this brings to an expected saving in setup times;
  - set-up times in cells 25% of the job shop one.
- The lot size can be half of the job shop case, thanks to the shorter set up times, obtaining lower WIP.
- These assumptions do not hold for those operations that are performed outside the due cell (the so called “exceptions”).

# MECHOFF – Draft solution

## Procedure

The following steps can be followed to find the best solution:

1. Use the **ROC algorithm** to identify the machine groups that will compose the cells;
2. Evaluate the **number of machines** of each type to be used in the cells;
3. Evaluate the **number of fixtures** that are needed for each product family (on each machine type within the cell).

# MECHOFF – ROC algorithm by King

Given:

$j$  = product index;

$P$  = number of products;

$i$  = machine index;

$M$  = number of machines;

$a_{ij}$  = 1 if product  $j$  needs operation on machine  $i$ ,

otherwise  $a_{ij} = 0$ ;

1. Per each row compute the rank number:

$$R_i = \sum_{j=1}^P (a_{ij} * 2^{P-j})$$

2. Reorder rows by decreasing values of  $R_i$  (top to bottom);
3. Per each column compute the rank number:

$$C_j = \sum_{i=1}^M (a_{ij} * 2^{M-i})$$

4. Reorder columns by decreasing values of  $C_j$  (left to right);
5. Repeat steps 1 to 4 until no reordering of columns or rows is needed.

# MECHOFF – Application of ROC (King)

In PRACTICE: having the products on rows or on columns is the same

		i=1,...,M						
		1	2	3	4	5		
		16	8	4	2	1		
j=1,...,P	2^(P-j)		M1	M2	M3	M4	M5	Rj
1	131072	PZ1	1	1	0	0	0	24
2	65536	PZ2	1	0	1	1	0	22
3	32768	PZ3	1	1	0	1	0	26
4	16384	PZ4	1	0	1	1	0	22
5	8192	DI1	1	1	0	1	1	27
6	4096	DI2	1	1	0	1	1	27
7	2048	DI3	1	0	0	1	1	19
8	1024	DI4	0	1	0	1	1	11
9	512	DI5	1	0	0	1	0	18
10	256	RO1	0	0	1	0	1	5
11	128	RO2	0	0	1	0	1	5
12	64	RO3	0	0	1	0	1	5
13	32	RO4	0	0	1	0	1	5
14	16	RO5	0	0	1	0	1	5
15	8	SP1	1	1	0	0	1	25
16	4	SP2	1	1	0	0	1	25
17	2	SP3	1	1	0	0	1	25
18	1	SP4	1	1	0	0	1	25

Rank rows

# MECHOFF – Application of ROC (King)

		M1	M2	M3	M4	M5	Rj reordered
131072	DI1	1	1	0	1	1	27
65536	DI2	1	1	0	1	1	27
32768	PZ3	1	1	0	1	0	26
16384	SP1	1	1	0	0	1	25
8192	SP2	1	1	0	0	1	25
4096	SP3	1	1	0	0	1	25
2048	SP4	1	1	0	0	1	25
1024	PZ1	1	1	0	0	0	24
512	PZ2	1	0	1	1	0	22
256	PZ4	1	0	1	1	0	22
128	DI3	1	0	0	1	1	19
64	DI5	1	0	0	1	0	18
32	DI4	0	1	0	1	1	11
16	RO1	0	0	1	0	1	5
8	RO2	0	0	1	0	1	5
4	RO3	0	0	1	0	1	5
2	RO4	0	0	1	0	1	5
1	RO5	0	0	1	0	1	5
	<b>Cj</b>	262080	261152	799	230368	227519	

- Reorder rows;
- Rank columns

# MECHOFF – Application of ROC (King)

	M1	M2	M4	M5	M3	Rj
DI1	1	1	1	1	0	30
DI2	1	1	1	1	0	30
PZ3	1	1	1	0	0	28
SP1	1	1	0	1	0	26
SP2	1	1	0	1	0	26
SP3	1	1	0	1	0	26
SP4	1	1	0	1	0	26
PZ1	1	1	0	0	0	24
PZ2	1	0	1	0	1	21
PZ4	1	0	1	0	1	21
DI3	1	0	1	1	0	22
DI5	1	0	1	0	0	20
DI4	0	1	1	1	0	14
RO1	0	0	0	1	1	3
RO2	0	0	0	1	1	3
RO3	0	0	0	1	1	3
RO4	0	0	0	1	1	3
RO5	0	0	0	1	1	3
Cj reordered	262080	261152	230368	227519	799	

- Reorder columns;
- Re-rank rows



# MECHOFF – Application of ROC (King)

	M1	M2	M4	M5	M3	R <sub>j</sub> reordered
DI1	1	1	1	1	0	30
DI2	1	1	1	1	0	30
PZ3	1	1	1	0	0	28
SP1	1	1	0	1	0	26
SP2	1	1	0	1	0	26
SP3	1	1	0	1	0	26
SP4	1	1	0	1	0	26
PZ1	1	1	0	0	0	24
DI3	1	0	1	1	0	22
PZ2	1	0	1	0	1	21
PZ4	1	0	1	0	1	21
DI5	1	0	1	0	0	20
DI4	0	1	1	1	0	14
RO1	0	0	0	1	1	3
RO2	0	0	0	1	1	3
RO3	0	0	0	1	1	3
RO4	0	0	0	1	1	3
RO5	0	0	0	1	1	3
<b>C<sub>j</sub></b>	<b>262080</b>	<b>261152</b>	<b>230368</b>	<b>227903</b>	<b>415</b>	

- Reorder rows;
- Re-rank columns



The order must not be changed:

→ this is the final matrix

# MECHOFF – Solution of ROC (King) 1

**Solution with no  
duplication of  
resources**

**Cell 1**

**Cell 2**

**Exceptions**

	M1	M2	M4	M5	M3
DI1	1	1	1	1	0
DI2	1	1	1	1	0
PZ3	1	1	1	0	0
SP1	1	1	0	1	0
SP2	1	1	0	1	0
SP3	1	1	0	1	0
SP4	1	1	0	1	0
PZ1	1	1	0	0	0
DI3	1	0	1	1	0
PZ2	1	0	1	0	1
PZ4	1	0	1	0	1
DI5	1	0	1	0	0
DI4	0	1	1	1	0
RO1	0	0	0	1	1
RO2	0	0	0	1	1
RO3	0	0	0	1	1
RO4	0	0	0	1	1
RO5	0	0	0	1	1

## MECHOFF – Solution of ROC (King) 2

**Solution with  
duplication of  
resources**

Cell 1

Cell 2

Exceptions

	M1	M2	M4	<i>M5 BIS</i>	M3	M5
DI1	1	1	1	1	0	0
DI2	1	1	1	1	0	0
PZ3	1	1	1	0	0	0
SP1	1	1	0	1	0	0
SP2	1	1	0	1	0	0
SP3	1	1	0	1	0	0
SP4	1	1	0	1	0	0
PZ1	1	1	0	0	0	0
DI3	1	0	1	1	0	0
PZ2	1	0	1	0	1	0
PZ4	1	0	1	0	1	0
DI5	1	0	1	0	0	0
DI4	0	1	1	1	0	0
RO1	0	0	0	0	1	1
RO2	0	0	0	0	1	1
RO3	0	0	0	0	1	1
RO4	0	0	0	0	1	1
RO5	0	0	0	0	1	1

## MECHOFF – Solution of ROC (King) 2

**Solution with  
duplication of  
resources**

**Cell 1**  
**Cell 2**  
**Exceptions**

**We take this  
configuration**

	M1	M2	M4	<i>M5 BIS</i>	M3	M5
DI1	1	1	1	1	0	0
DI2	1	1	1	1	0	0
PZ3	1	1	1	0	0	0
SP1	1	1	0	1	0	0
SP2	1	1	0	1	0	0
SP3	1	1	0	1	0	0
SP4	1	1	0	1	0	0
PZ1	1	1	0	0	0	0
DI3	1	0	1	1	0	0
PZ2	1	0	1	0	1	0
PZ4	1	0	1	0	1	0
DI5	1	0	1	0	0	0
DI4	0	1	1	1	0	0
RO1	0	0	0	0	1	1
RO2	0	0	0	0	1	1
RO3	0	0	0	0	1	1
RO4	0	0	0	0	1	1
RO5	0	0	0	0	1	1

# MECHOFF – Division of products in cells

Cell	Product	
1	DI1	
	DI2	
	PZ3	
	SP1	
	SP2	
	SP3	
	SP4	
	PZ1	
	DI3	
	PZ2	***
	PZ4	***
	DI5	
	DI4	
2	RO1	
	RO2	
	RO3	
	RO4	
	RO5	

Once defined the cell (Product Families and Machine types), dimensioning is carried out with exactly the same approach of job-shop dimensioning, but:

- Setup time is lower in the same cell for each product family (even = 0), due to common machinery fixture :  $\frac{1}{4}$  of the job shop setup time
- Smaller lots:  $\frac{1}{2}$  of the job shop lots  $\rightarrow$  lower Lead Time and WIP

\*\*\* exceptional products

# MECHOFF – Cell dimensioning

As in the job shop case, the formula for the required capacity is the following:

$$NH_i = \sum_{j=1}^N \left( \frac{T_{ij} \cdot Q_j}{3600 \cdot (1 - SR_{ij})} + \frac{STT_{ij}}{60} \cdot NL_j \right) \cdot \frac{1}{A_i} \cdot \frac{1}{HC_i} \cdot \frac{1}{TR_i}$$

Where:

- $i$  = index of the machine-type
- $j$  = index of the product-type
- $N$  = number of different product-types
- $T_{ij}$  = unit working time [seconds/piece]
- $Q_j$  = quantity of product-type  $j$  that has to be produced [pieces/year]
- $SR_{ij}$  = scrap rate ( $0 \leq SR_{ij} < 1$ )
- $STT_{ij}$  = setup time [minutes/setup]
- $NL_j$  = number of lots of product-type  $j$  [lots/year]
- $A_i$  = availability ( $0 < A_i \leq 1$ )
- $HC_i$  = human coefficient ( $0 < HC_i \leq 1$ )
- $TR_i$  = trial rate ( $0 < TR_i \leq 1$ )

# MECHOFF – Cell dimensioning

As in the job shop case, the required capacity must be compared to the available capacity.

Each machine has the following available capacity:

$$AH_i(s) = WH_i(s) \cdot SE$$

where:

$WH_i(s)$  = yearly working time available (depending on the number of shifts/day)

$SE$  = scheduling efficiency ( $0 < SE \leq 1$ ), in this case it is equal to 0.85

**WH** = (7.5 hours/shift \* 2 shifts \* 220 days/year) = 3300 hours/year

**SE** = 0.85

**AH** =  $WH * SE = 2805$  hours/year

# MECHOFF – Cell 1 dimensioning

	M1			M2			M4			M5 bis	
	Annual required working hours	Annual required setup hours		Annual required working hours	Annual required setup hours		Annual required working hours	Annual required setup hours		Annual required working hours	Annual required setup hours
DI1	518	40	DI1	518	30	DI1	389	40	DI1	1295	20
DI2	705	30	DI2	1409	20	DI2	493	60	DI2	3523	10
PZ3	207	18	PZ3	259	27	PZ3	337	22,5	PZ3	0	0
SP1	2591	18,75	SP1	1554	6,25	SP1	0	0	SP1	6218	25
SP2	3264	17,5	SP2	3627	17,5	SP2	0	0	SP2	5803	26,25
SP3	808	7,8	SP3	539	9,75	SP3	0	0	SP3	2425	6,5
SP4	1244	20	SP4	1658	20	SP4	0	0	SP4	3109	20
PZ1	285	15	PZ1	648	15	PZ1	0	0	PZ1	0	0
DI3	1943	22,5	DI3	0	0	DI3	1101	30	DI3	4534	15
PZ2	130	4,5	PZ2	0	0	PZ2	104	6	PZ2	0	0
PZ4	207	4,5	PZ4	0	0	PZ4	181	6,75	PZ4	0	0
DI5	104	7,5	DI5	0	0	DI5	104	22,5	DI5	0	0
DI4	0	0	DI4	5181	25	DI4	1295	25	DI4	1036	6,25
	Total	13390		Total	17066		Total	4623		Total	30781

**Number of machines = total required hours / available hours (rounded to the next integer)**

$$M1 = 13390 / 2805 = 5$$

$$M2 = 17066 / 2805 = 7$$

$$M4 = 4623 / 2805 = 2$$

$$M5 \text{ bis} = 30781 / 2805 = 11$$



# MECHOFF – Cell 2 dimensioning

		<b>M5</b>	
		Annual required working hours	Annual required setup hours
RO1		4145	37,5
RO2		492	7,5
RO3		6601	25
RO4		544	15
RO5		6736	100
		<b>Total</b>	<b>20508</b>

		<b>M3</b>	
		Annual required working hours	Annual required setup hours
RO1		3316	15
RO2		155	5
RO3		6736	10
RO4		104	11
RO5		5181	50
PZ2		259	36
PZ4		648	49,5
		<b>Total</b>	<b>18175</b>

**Number of machines = total required hours / available hours (rounded to the next integer)**

$$M5 = 20508 / 2805 = 8$$

$$M3 = 18175 / 2805 = 7$$

# MECHOFF – Fixture dimensioning

The ratio behind the fixture dimensioning is the same as the cell dimensioning:

***Required hours vs available hours (on each machine type)***

The formulas are as usual:

and

$$NH_i = \sum_{j=1}^N \left( \frac{T_{ij} \cdot Q_j}{3600 \cdot (1 - SR_{ij})} + \frac{STT_{ij}}{60} \cdot NL_j \right) \cdot \frac{1}{A_i} \cdot \frac{1}{HC_i} \cdot \frac{1}{TR_i}$$

$$AH_i(s) = WH_i(s) \cdot A\_fixture$$

where the parameters have the same meaning as in the machine case.

Please note that:

- $A_i=1$ , availability (of the machine) is considered 1 because fixtures are used only when machines are available while they are removed from the machines when maintenance actions are performed leading to machine unavailability;
- $A\_fixture$  is here considered as a coefficient to represent that the fixture has to be maintained; hence its availability is set at 0,98.

Therefore:

$$AH = (7.5 \text{ hours/shift} * 2 \text{ shifts} * 220 \text{ days/year}) * 0,98 = 3234 \text{ hours/year}$$

# MECHOFF – Fixture dimensioning for DI product family

		M1		M2		M4		M5 bis	
		Annual required working hours	Annual required setup hours	Annual required working hours	Annual required setup hours	Annual required working hours	Annual required setup hours	Annual required working hours	Annual required setup hours
DI1		518	40	518	30	389	40	1295	20
DI2		705	30	1409	20	493	60	3523	10
DI3		1943	22,5	0	0	1101	30	4534	15
DI5		104	7,5	0	0	104	22,5	0	0
DI4		0	0	5181	25	1295	25	1036	6,25
		Total	3510	Total	7483	Total	3708	Total	10875

**Number of fixture = total required hours / available hours (rounded to the next integer)**

Number of fixtures for DI product family:

$$M1 = 3510 / 3234 = 2$$

$$M2 = 7483 / 3234 = 3$$

$$M4 = 3708 / 3234 = 2$$

$$M5 \text{ bis} = 10875 / 3234 = 4$$

# MECHOFF – Fixture dimensioning for PZ product family

		M1		M2		M4		M5 bis				
		Annual required working hours	Annual required setup hours	Annual required working hours	Annual required setup hours	Annual required working hours	Annual required setup hours	Annual required working hours	Annual required setup hours			
<b>PZ3</b>		207	18	<b>PZ3</b>	259	27	<b>PZ3</b>	337	22,5	<b>PZ3</b>	0	0
<b>PZ1</b>		285	15	<b>PZ1</b>	648	15	<b>PZ1</b>	0	0	<b>PZ1</b>	0	0
<b>PZ2</b>		130	4,5	<b>PZ2</b>	0	0	<b>PZ2</b>	104	6	<b>PZ2</b>	0	0
<b>PZ4</b>		207	4,5	<b>PZ4</b>	0	0	<b>PZ4</b>	181	6,75	<b>PZ4</b>	0	0
		Total	907	Total	988	Total	684	Total		0		

**Number of fixture = total required hours / available hours (rounded to the next integer)**

Number of fixtures for PZ product family

$$M1 = 907 / 3234 = 1$$

$$M2 = 988 / 3234 = 1$$

$$M4 = 684 / 3234 = 1$$

$$M5 \text{ bis} = 0$$

# MECHOFF – Fixture dimensioning for SP product family

		M1		M2		M4		M5 bis	
		Annual required working hours	Annual required setup hours	Annual required working hours	Annual required setup hours	Annual required working hours	Annual required setup hours	Annual required working hours	Annual required setup hours
SP1		2591	18,75	1554	6,25	0	0	6218	25
SP2		3264	17,5	3627	17,5	0	0	5803	26,25
SP3		808	7,8	539	9,75	0	0	2425	6,5
SP4		1244	20	1658	20	0	0	3109	20
		Total	8303	Total	7741	Total	0	Total	18367

**Number of fixture = total required hours / available hours (rounded to the next integer)**

Number of fixtures for SP product family

$$M1 = 8303 / 3234 = 3$$

$$M2 = 7741 / 3234 = 3$$

$$M4 = 0$$

$$M5 \text{ bis} = 18367 / 3234 = 6$$

# MECHOFF – Fixture dimensioning for RO product family

M5		
	Annual required working hours	Annual required setup hours
RO1	3316	15
RO2	155	5
RO3	6736	10
RO4	104	11
RO5	5181	50
	Total	16233

M3		
	Annual required working hours	Annual required setup hours
RO1	4145	37,5
RO2	492	7,5
RO3	6601	25
RO4	544	15
RO5	6736	100
	Total	19482

**Number of fixture = total required hours / available hours (rounded to the next integer)**

Number of fixtures for RO product family

$$M5 = 16233 / 3234 = 6$$

$$M3 = 19482 / 3234 = 7$$

# MECHOFF – Economic Assessment – Concluding Remarks

Investment cost	Needed Machines	Existing Machines	No. Of new machines	Machine cost (euros)	Machine lifetime indicator	Yearly cost
M1	5	2	3	150000	0,05	22,500
M2	7	5	2	300000	0,05	30,000
M3	7	8	-1	200000	0,05	-
M4	2	2	0	250000	0,05	-
M5	19	12	7	250000	0,05	87,500
<b>Total Investment cost</b>						<b>140,500</b> Euro/year

  

Operator cost	no. Of machines	no.of operators per shift
Cell 1	25	13
Cell 2	15	8
<b>Total</b>		21
<b>Current</b>		15
<b>no. Of operators more per shift</b>		6
<b>Labor cost</b>		<b>277,200</b> Euro/year

  

**Total cost =**  
 $140000 + 277200 =$   
**417,200 Euro/year**

## Remarks:

- 1) This cost does not include the fixture costs;
- 2) The economic assessment on machines and labour allows to verify the cost of a **STRATEGIC DECISION** aimed at gaining benefits in quality and delivery performance.