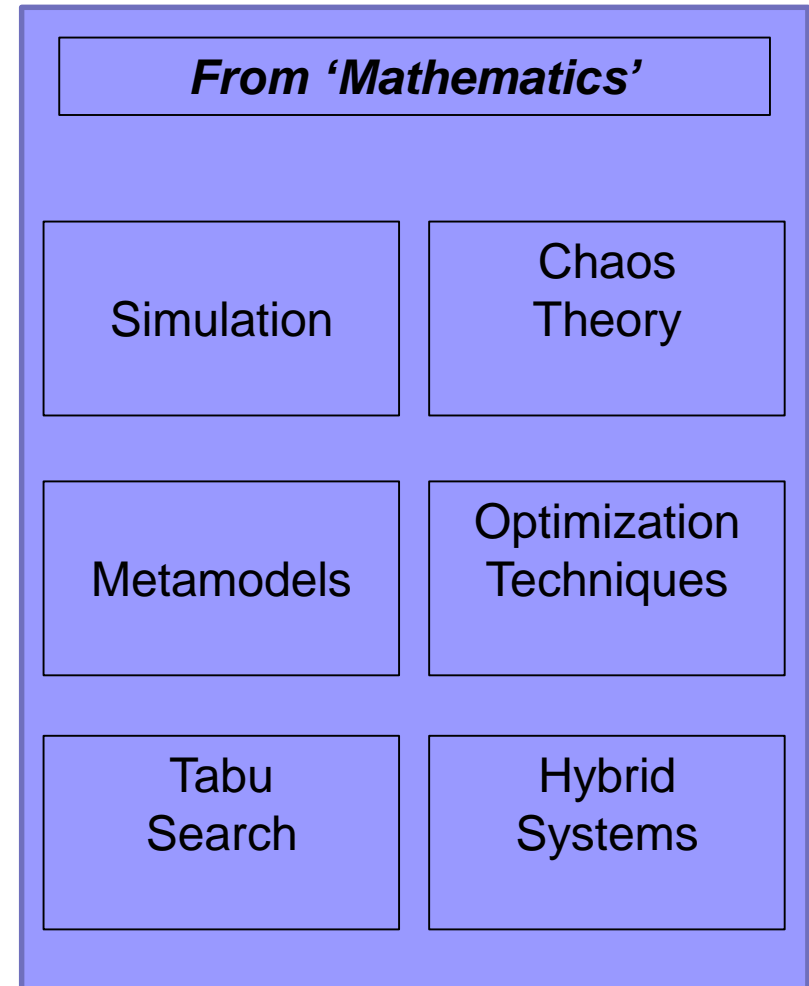
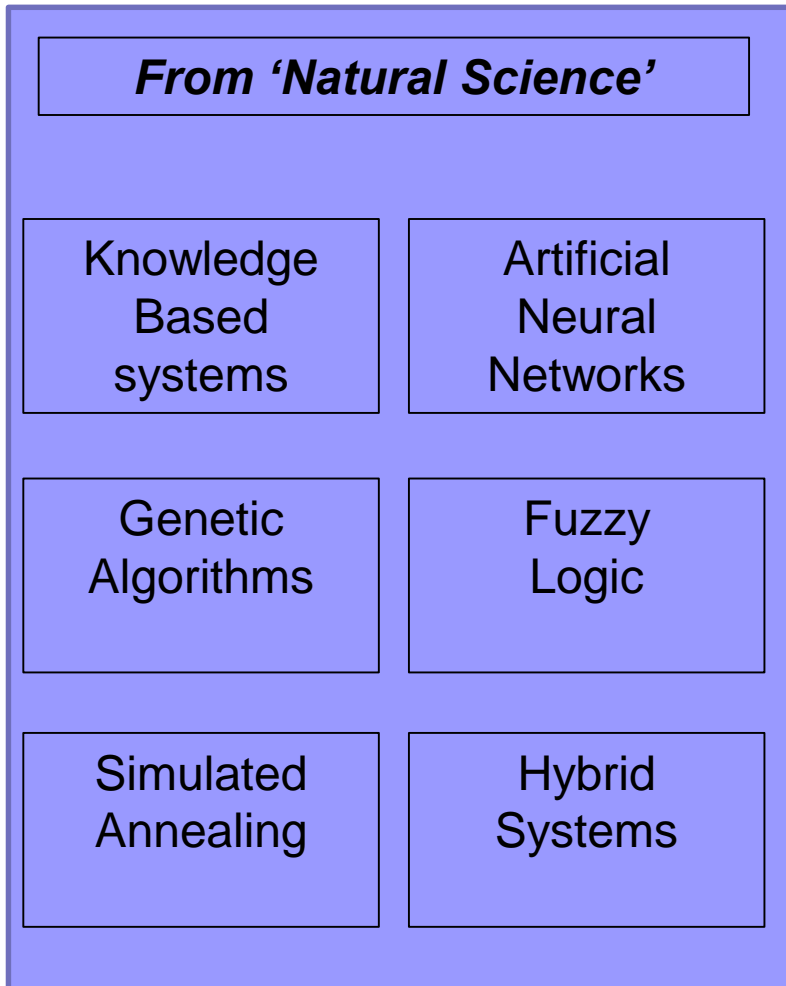


# Advanced techniques for design and management of production systems

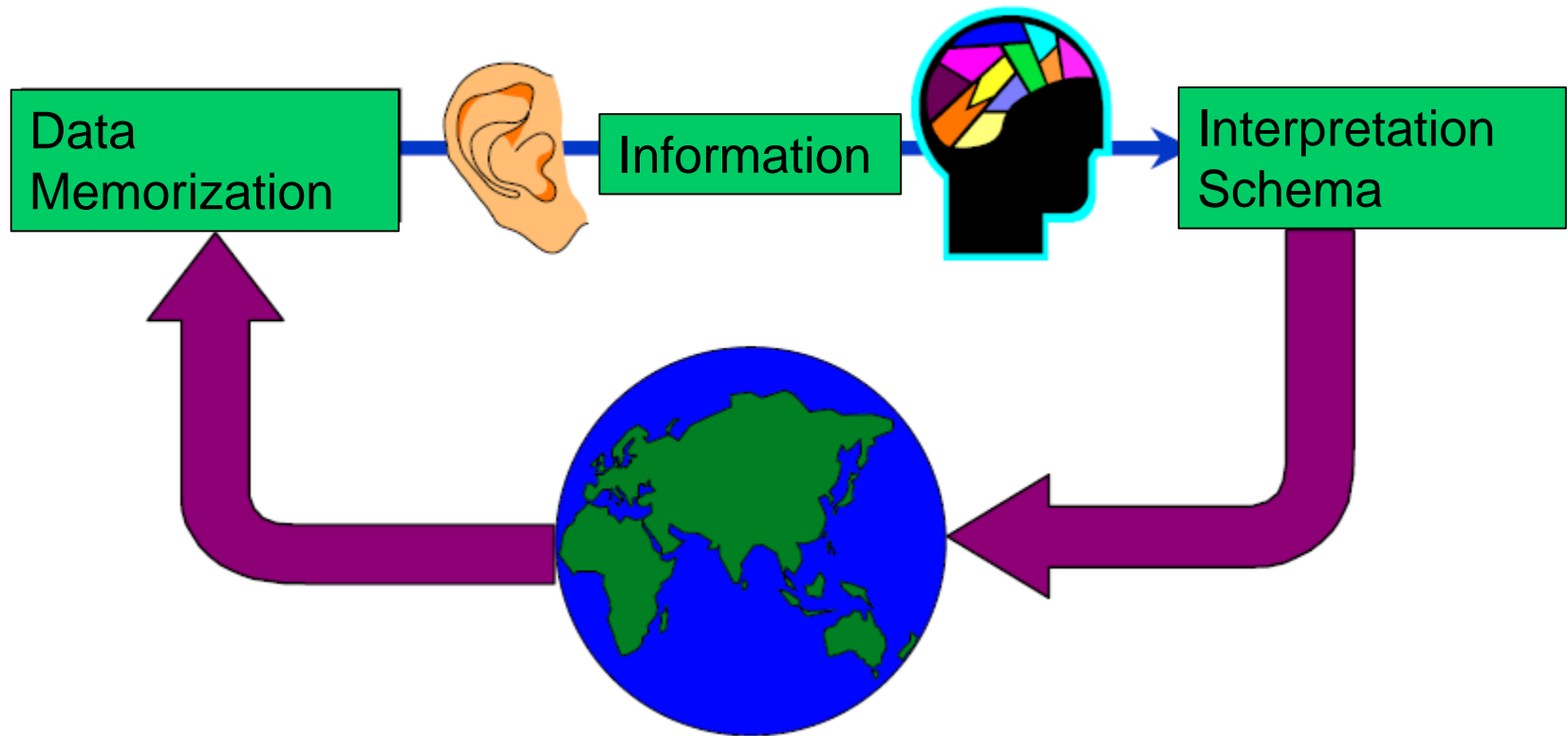
# General overview



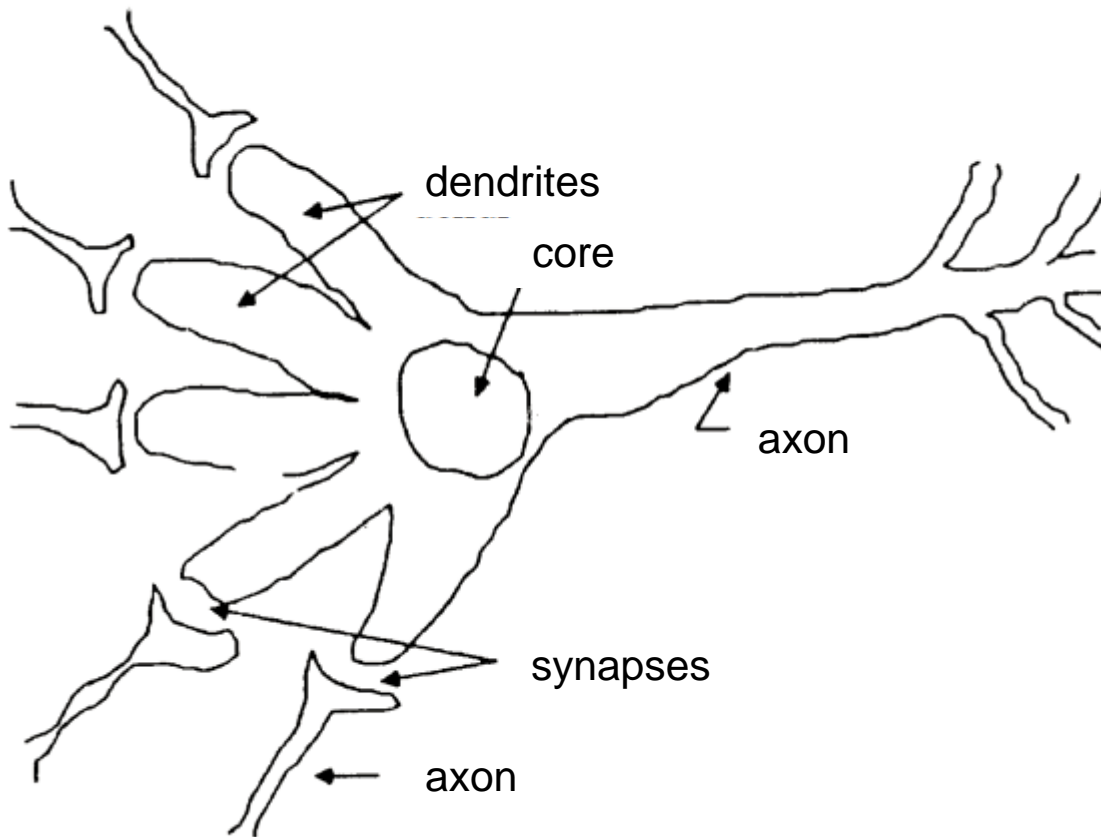


# Artificial Neural Networks

# Knowledge acquisition process

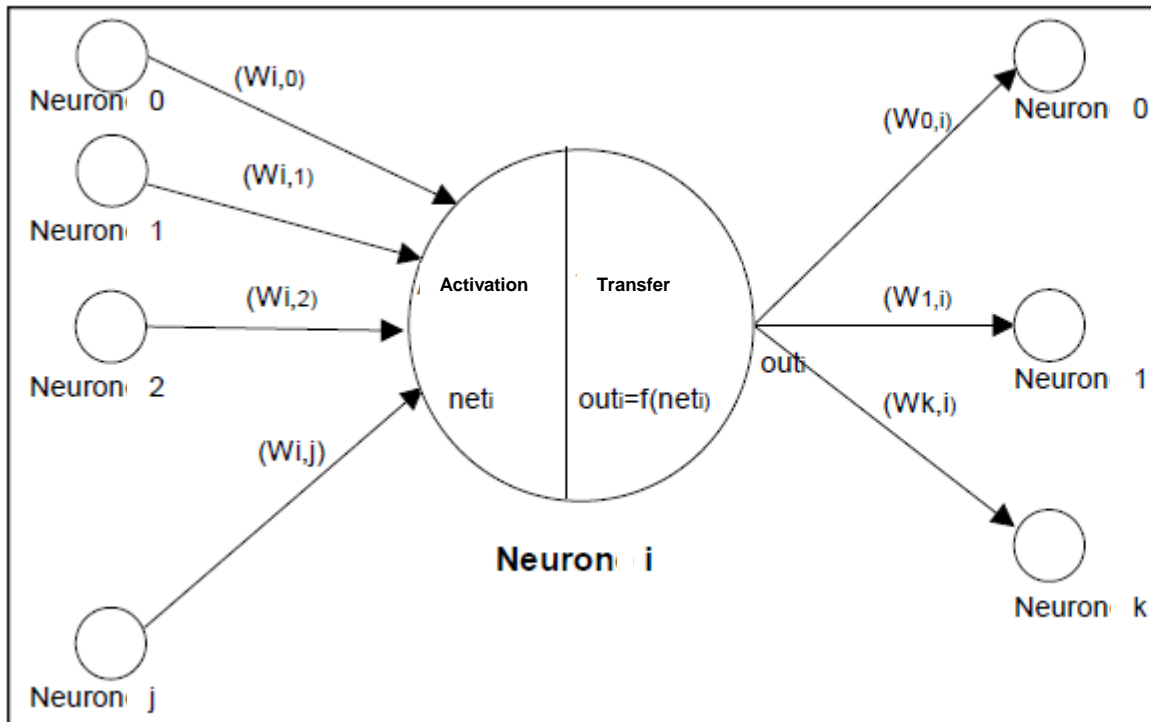


# The biological neuron



- Human brain contains  $10^{12}$  neurons
- Neuron dimensions from 0.01 mm to 1 m (depending on axon length)
- Connectivity of a single neuron from  $O(1)$  to  $O(10^5)$ : the number of synapses is  $O(10^{15})$

# The artificial neuron



$$net_i = \sum_j w_{i,j} out_j + \mathcal{I}_i$$

$$out_i = f(net_i)$$

$i$  = index of generic neuron

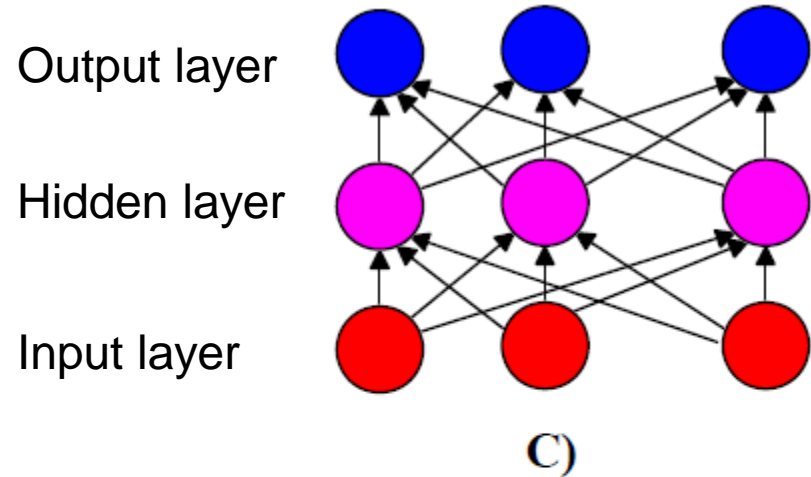
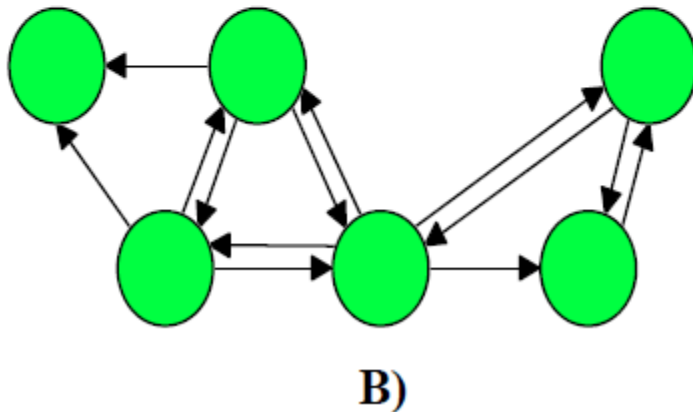
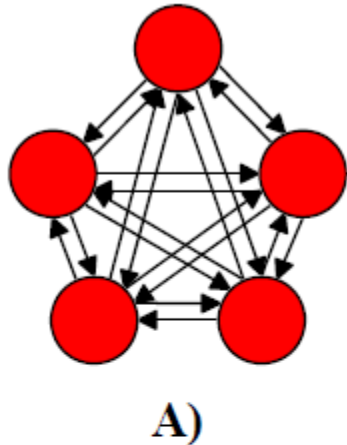
$j$  = index of generic neuron in input to neuron  $i$

$k$  = index of generic neuron in output from neuron  $i$

$j$  into  $S_{input}$  (set of input neurons to  $i$ )

$k$  into  $S_{output}$  (set of output neurons from  $i$ )

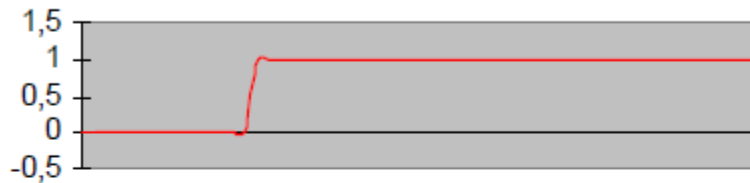
# Topologies of ANN



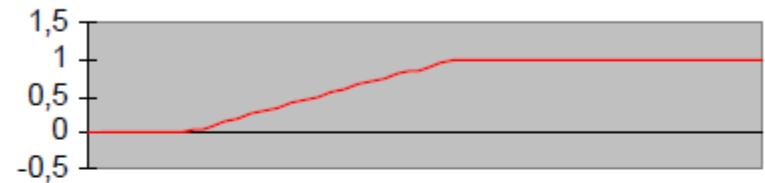
- A) Completely interconnected
- B) Partially connected
- C) In layers

# Transfer functions

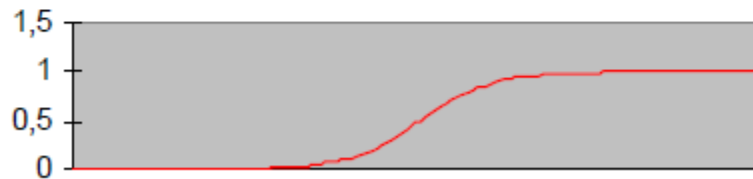
Step



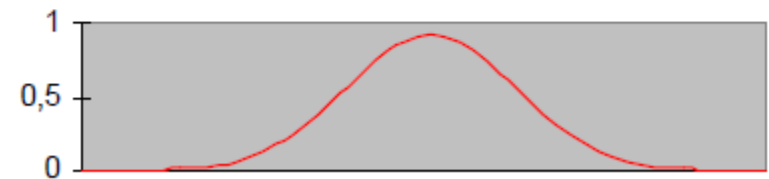
Ramp



Sigmoidal



Gaussian



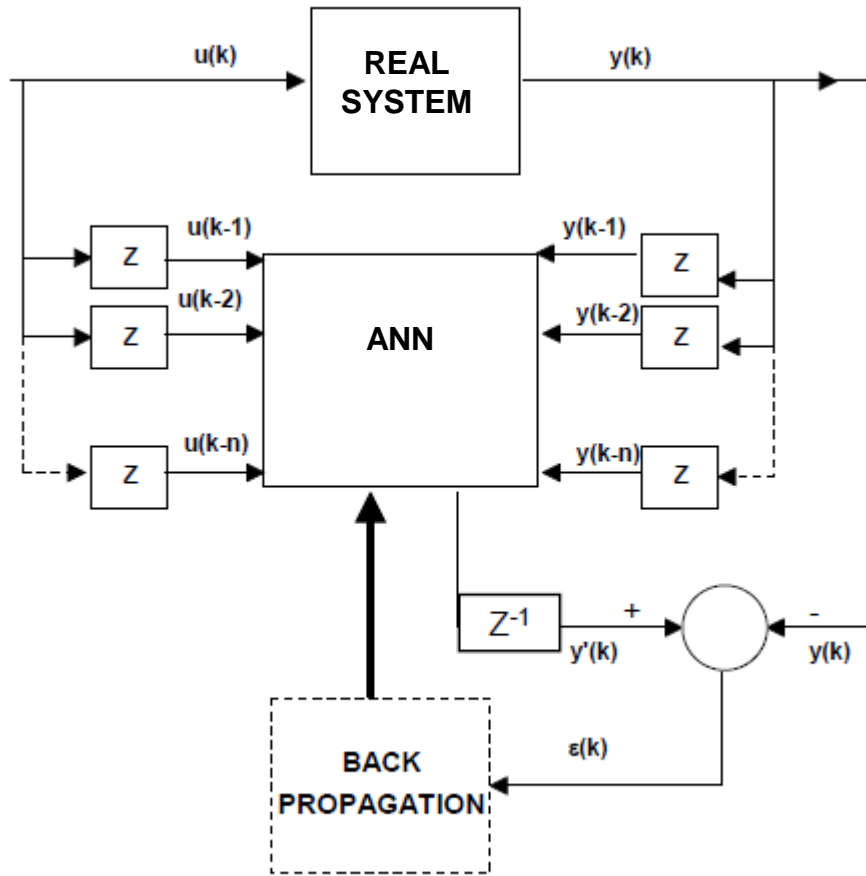


# Knowledge and learning

- Knowledge is not defined by rules (like Knowledge-based Systems), but is distributed into values of connection weights.
- Learning processes:
  - Supervised
  - Not supervised
  - Fixed weights
- Learning occurs on the basis of specific algorithms which update the weights of connections.
- Hebb law:

$$W_{i,j}(t+1) = W_{i,j}(t) + \Delta W_{i,j}$$

# Supervised learning



The goal is the minimization of the following cost function:

$$E = \frac{1}{2} \sum_{n=1}^N (y'_n(t) - y_n(t))^2$$

where  $y'_n(t)$  is the value of output  $n$  computed by ANN, with an input  $u(t)$

At each iteration the connection weight is changed by using the following law:

$$\Delta w_{ij}(t) = -\eta \cdot \frac{\partial E(t)}{\partial w_{ij}(t)} + \alpha \cdot \Delta w_{ij}(t-1)$$

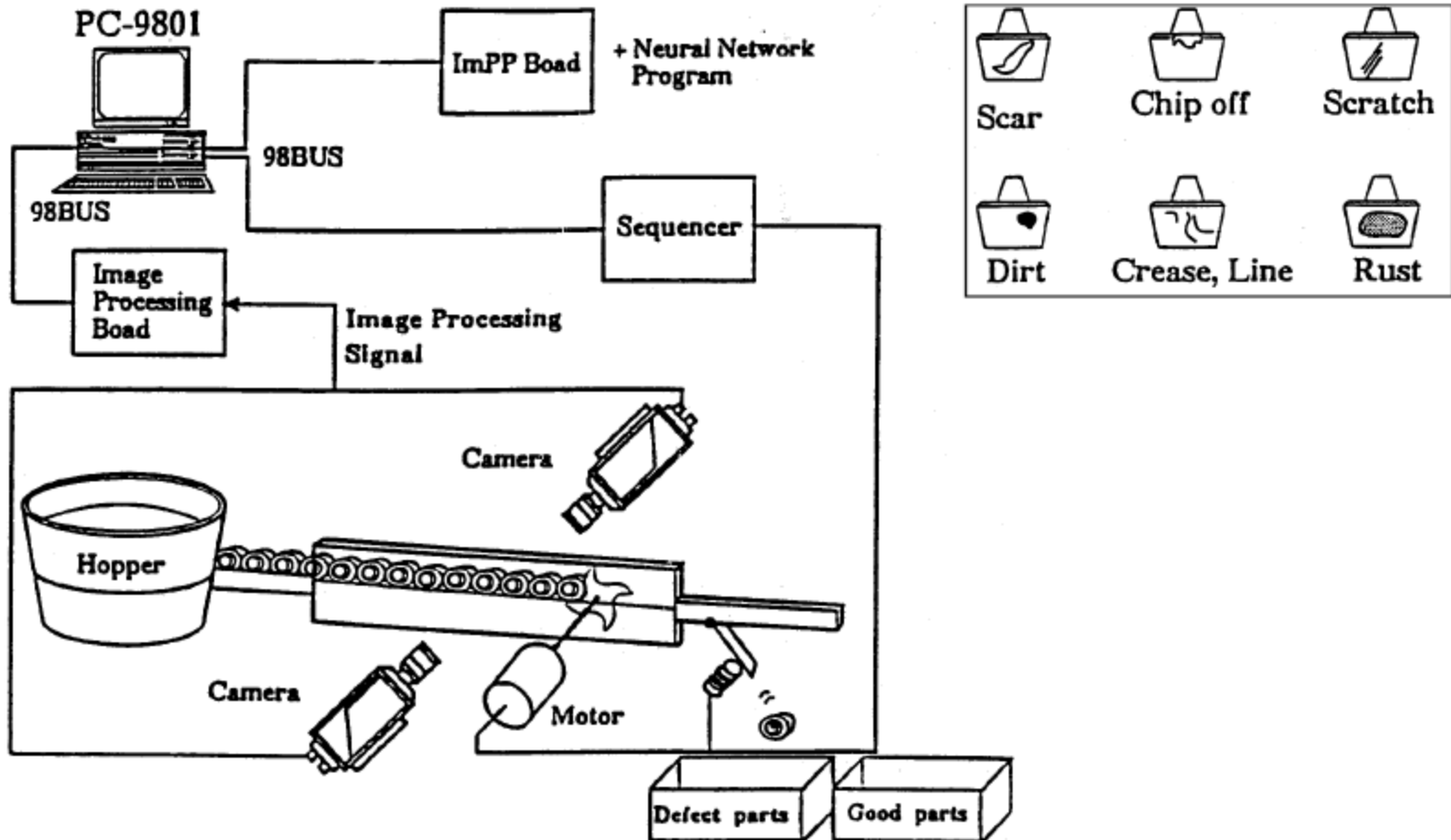
Where:

- $\eta$  is the learning coefficient
- $\alpha$  is the inertia coefficient

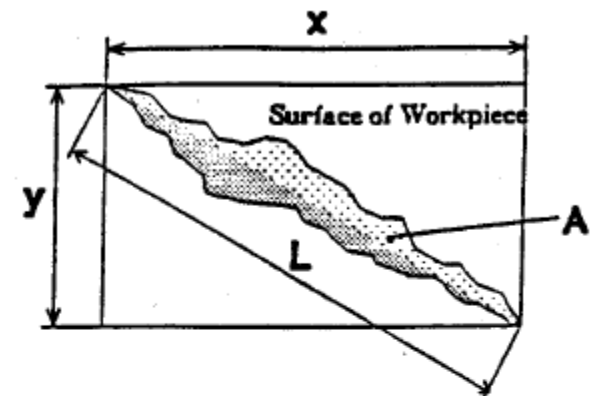
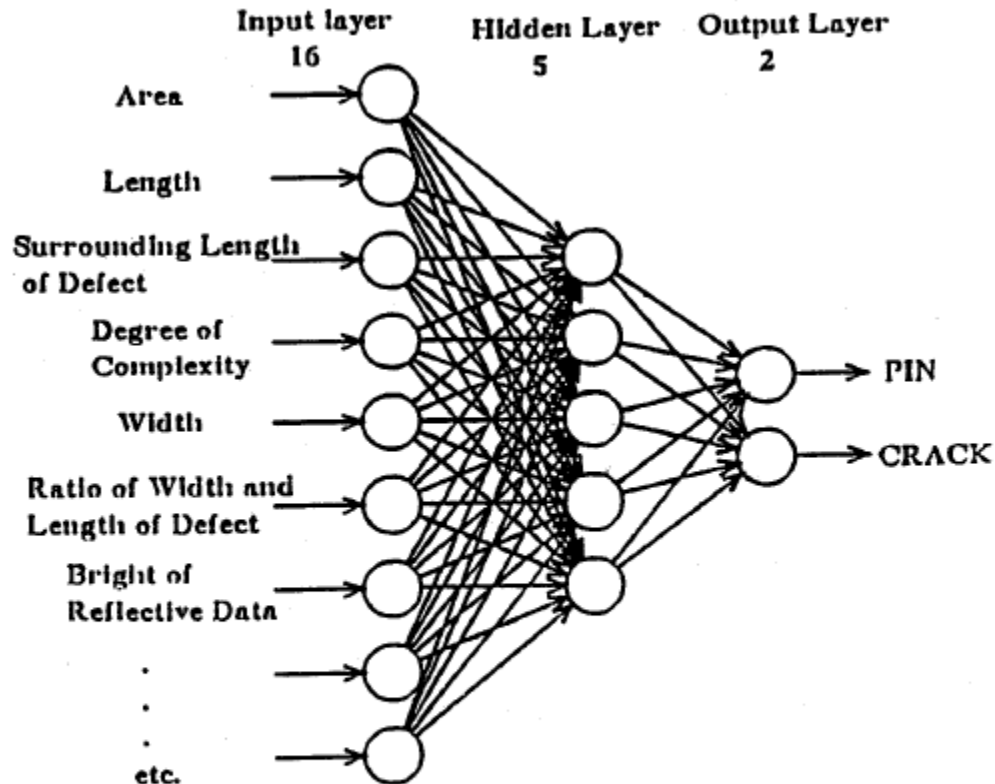
# Applications

- Classification and recognition: e.g. OCR, quality control in production, medical analysis, ...
- Forecast: loan approval, financial market, ...
- Optimization: delivery path, production management, ...
- Control: robot movement, industrial process control, vehicle control

# An example



# An example



An Example of Crack

## Features

1. Area of Defect :  $A$
2. Length of Defect :  $L$
3. Surrounding Length of Defect :  $S$
4. Degree of Complexity :  $\theta = L^2 / A$
5. Ratio of Width and Length of Defect :  $S/L$
6. Brightness of Reflective Data
7. Color of Defect
8. Feature of Surrounding Line of Defects



# ANN advantages

- Data-driven and not model-driven
- Easy to use
- Lower costs than other techniques
- It is possible to solve problem currently not solveable automatically



# Knowledge-based systems

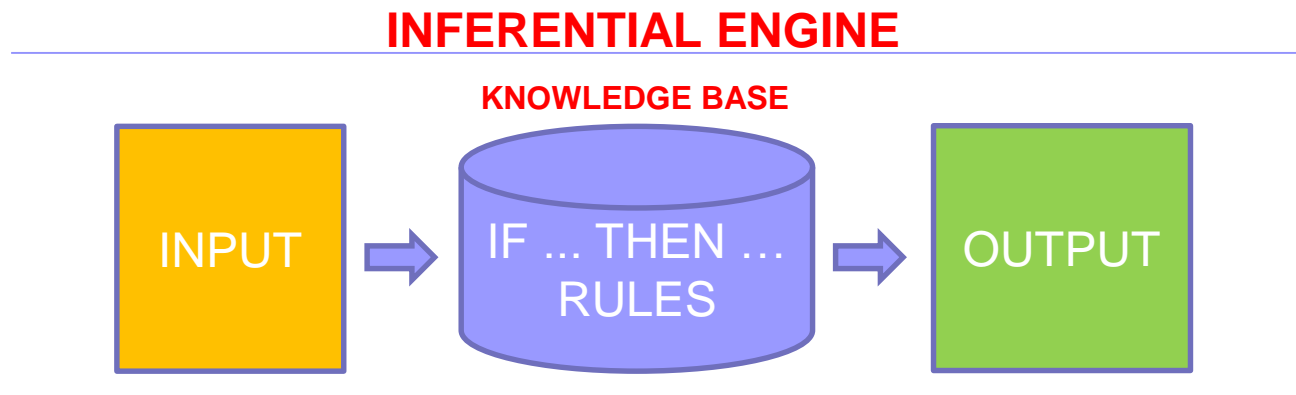
# Knowledge-based systems

- Software programs that are able to deduce informations from a set of starting input data
- They are based on human competence, registered into a so called 'knowledge base'
- It is possible to operate on incomplete and qualitative data (e.g. "fuzzy logic")
- It is always possible to explain the decisions of the knowledge-based system (Glass Box)



# Knowledge-based systems

- It is composed of two elements:
  - KNOWLEDGE BASE: facts that happen in real life; it represents the knowledge of an operator
  - INFERENCE ENGINE: a mechanism that analyze the data in input to the system, in order obtain conclusions from the observed facts.



# Knowledge-based systems types

## ■ Based on rules

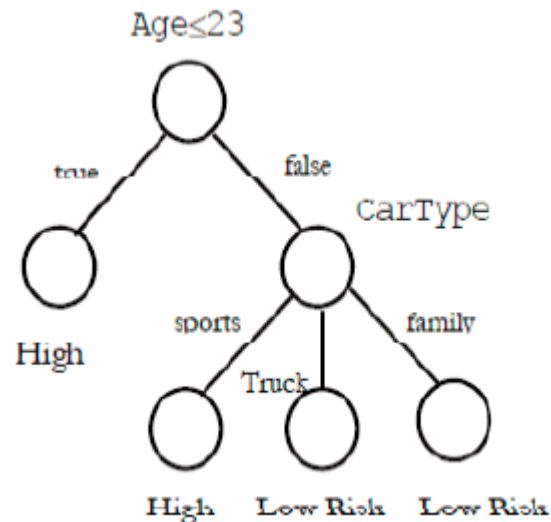
- They are programs composed of 'IF condition THEN action' rules. Given a set of facts, knowledge-based systems, due to rules application, can deduce new facts.

## ■ Based on trees:

- From a set of data and some deductions, a decision tree is defined in order to classify the input data. New informations are analyzed by the tree and the arrival node represents the decision.

# Examples

- Example of tree:



- Example of rule:

- Input data set:

- Headache

- Cold

- Temperature 38° C

- Rule:

IF *headache* AND *cold* AND  
*temperature*>37°C AND  
*temperature*<38.5°C THEN *flu*

# Knowledge-based systems design

- The knowledge-based system use the defined rules, but cannot create them. Hence during design phase it is necessary to define:
  - The logical structure
  - The data types
  - The sets and the classes
  - The limits
  - The IF...THEN... rules

# An example

IF (vel IS 120) AND (limit is 50) AND (autovelox IS present)  
THEN (reaction IS slowdown)

- The logical structure: triple IF
- The data types:
  - Vel: float
  - Limit: integer
  - Autovelox: boolean (present/not present)
  - Reaction: 3 state (slowdown, mantain, accelerate)
- The sets/classes and limits:
  - Vel: from 0 to 220
  - Limit: 30, 50, 70, 90, 110, 130

# Advantages vs problems

- Same responses in case of repeated decisions
- Glass box
- Contains several data and informations
- The decision can always be clearly explained
- Every aspects included are analyzed: nothing is forgotted or leaved out
- Important data can be leaved out from design
- Not useful in case of unexpected facts
- Cost to exctract knowledge from operators.
- Bad design = bad decisions
- Cannot be adapted in case of environment changes



# Fuzzy logic

# Fuzzy logic

- L.A. Zadeh
- It is a mathematical theory introduced in order to model uncertainty
- It is an extension of Aristotelian logic (a.k.a. crisp logic)

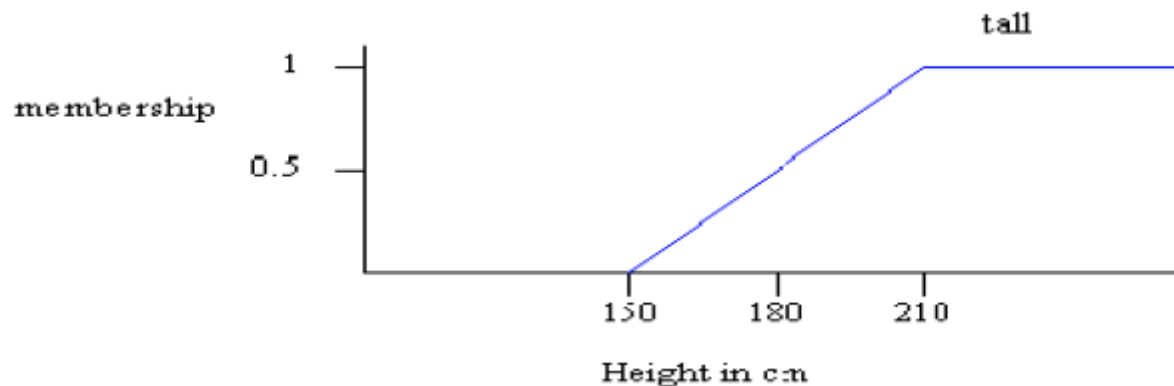


# Aristotelian logic

- Principle of excluded middle (third excluded): an element cannot belong at the same time to a set and its complement.
- Principle of non-contradiction: a statement can be only true or false

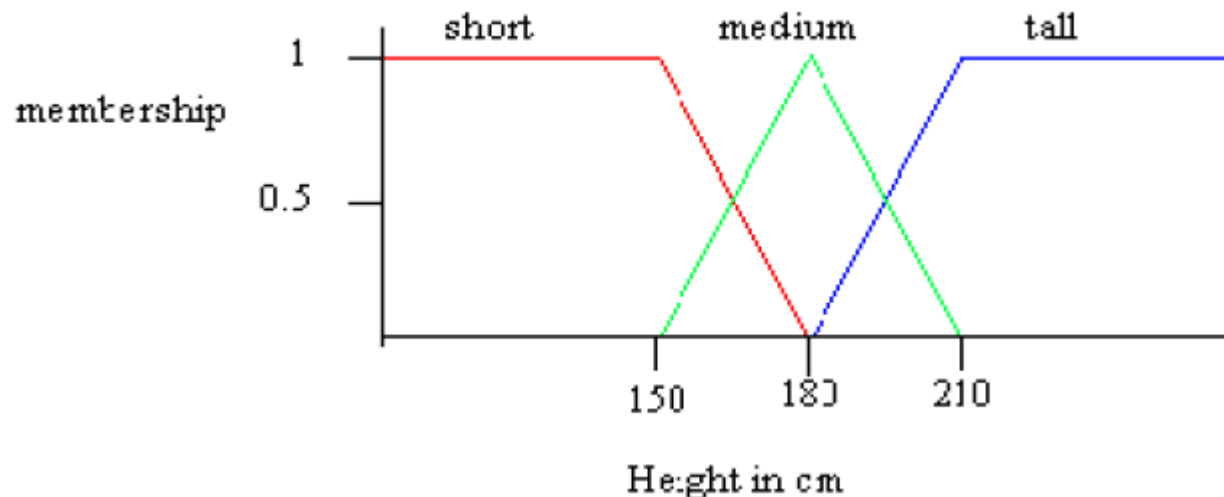
# Fuzzy logic

- In real life (natural language) it is difficult to have statement that can be only true or false. E.g. Am I old? Am I tall?
- The truth level (membership) can be represented with a value from 0 to 1 (with 0 and 1 the logic is the same as Aristotelian)



# Uncertainty representation

- If an element belongs to a set, this does not mean that it cannot belong to its complement.



# Real life and uncertainty

- Height, wealth, heat, speed, difficulty: they are all vague concepts.
- The semantics of the natural language can represent this aspect:
  - The soaked road
  - The wet road
  - The dry road

# Fuzzy logic and knowledge-based system

- Fuzzy logic is able to represent the typical situations of a human being.
- It is very useful in order to create knowledge-based Systems, that have to respond like a human being
- The IF ... THEN ... rules can be defined by using fuzzy logic
  - IF soaked road THEN go slowly
  - IF wet road THEN go a little bit slowly
  - IF awash road THE go very slowly

# Fuzzy logic advantages

- It operates with the same logic as humans, with vague concepts and with uncertainty
- It allows to code the technical knowledge without defining with precision the limits of rules.
- It allows to represent rules by using common language and not numerical sets (aligned with expert knowledge).
- Soft transition to one rule to another one (more than one rule can be applied, with different levels of truth).



# Fuzzy logic disadvantages

- Identification of the complete set of rules
- Risk to create an inaccurate and incomplete knowledge base
- Long time in order to obtain a good knowledge base