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СПППОЮБУ

To Put It int Practice

Lesson X: International Portfolio Investments

Monday 20th May, 2019



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► Portfolio Expected Return

$$E[r_p] = \sum_{i=1}^n x_i \cdot E[r_i]$$

► Portfolio Variance

$$Var[r_{\rho}] = \sum_{i=1}^{n} x_i^2 \cdot \sigma_i^2 + \sum_{i=1}^{n} \sum_{j \neq i=1}^{n} x_i \cdot x_j \cdot \sigma(i,j)$$

Can you spot the diversification-related terms?



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$$\sum_{i=1}^{n} \sum_{j\neq i=1}^{n} x_i \cdot x_j \cdot \sigma(i,j)$$



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The portfolio standard deviation is reduced if the correlation terms are **negative**, but, even when they are **positive**, the portfolio standard deviation is still less than the weighted average of the individual securities standard deviations

To Make Matters Explicit

	Stock a	Stock b
E[r]	0.08	0.055
StDev	0.15	0.1
Weights	0.75	0.25

$\rho(a,b)$	$E[r_p]$	Risk _p	WRisk _p
-1	0.07375	0.0875	0.1375
-0.5	0.07375	0.1023	0.1375
-0.2	0.07375	0.1103	0.1375
0	0.07375	0.1152	0.1375
0.2	0.07375	0.12	0.1375
0.5	0.07375	0.1269	0.1375
1	0.07375	0.1375	0.1375

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A Few Key Points to Retain

Portfolios of **less than perfectly** correlated assets always offer better risk-return opportunities than the individual constituent securities on their own.



What about **perfect positive** correlations?



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The Risk-Return Framework

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The Risk-Return-Correlation Framework

Assuming risk aversion, investors demand higher returns for taking on higher risk.



Remember: Risk relates to returns' volatility - variability over a given time period (generally defined as standard deviation of returns)⇒ Step back to Lesson IX

Portfolio Selection Criteria

How to select the most suitable combination of assets so as to maximize portfolio return for a given level of risk?

Focus on the triplet: Risk-Return-Correlation



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Portfolio Investment with 2 Risky Assets and Correl= -0.5

Suppose there are only 2 risky assets on the market (a and b, $\rho(a,b)=-0.5$) and assume further that:

Constituents	E[r]	StDev
a	0.08	0.15
b	0.055	0.1

Depending on the different weighting schemes below, would you be able to find the Expected Return and the Standard Deviation of the portfolio?

W_a		W_b	$E[r_p]$	$StDev_p$
1		0		
0.75	5	0.25		
0.5		0.5		
0.25	5	0.75		
0		1		

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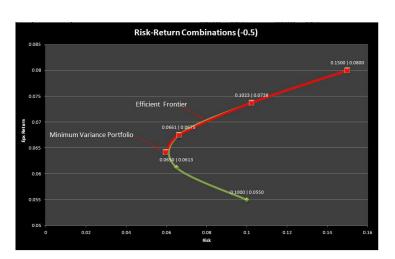
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Portfolio Investment with 2 Risky Assets and Correl= 0.2

Assume now that $\rho(a,b) = 0.2$: given the different weighting schemes below, would you be able to find the Expected Return and the Standard Deviation of the portfolio?

W_a	W_b	$E[r_p]$	$StDev_p$
1	0		
0.75	0.25		
0.5	0.5		
0.25	0.75		
0	1		



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In Graphical Terms - Inter-Asset Correlation=0.2

0.06

0.05

0.02

0.04

0.06

0.08





0.10001 0.0550

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0.14

0.16

Portfolio Investment with 2 Risky Assets and Correl= 0

Assume now that $\rho(a,b)=0$: given the different weighting schemes below, would you be able to find the Expected Return and the Standard Deviation of the portfolio?

W_a	W_b	$E[r_p]$	$StDev_p$
1	0		
0.75	0.25		
0.5	0.5		
0.25	0.75		
0	1		



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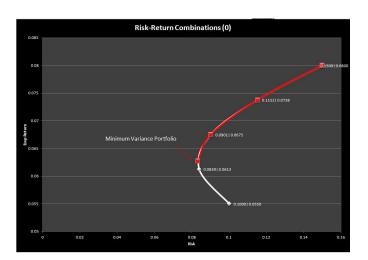
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In Graphical Terms - Inter-Asset Correlation=0



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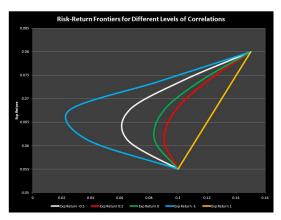
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Wrapping Up

The **shape** of the frontier varies depending on **inter-assets correlations**.



The final portfolio selection will depend **exclusively** on individual risk appetite

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Suppose there are only 2 risky assets on the market (a and b, $\rho(a,b) = -0.5$ - step back to the previous section) and a riskless portfolio (made up of MM instruments and Govt Bonds), yielding 0.05.

How to determine which **optimal risky portfolio is to be best combined with the riskless** security basket?

Adopted Selection Criteria: Max[REWARD to RISK]



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To Put It into

Assume you invest a proportion of your total wealth (α) in the risky portfolio $(E[r_{risky}])$ and the remaining portion of your investable K $((1-\alpha))$ in the riskless asset (yielding $r_{riskless}$):

► Portfolio Expected Return

$$E[r_p] = \alpha E[r_{risky}] + (1 - \alpha)r_{riskless} = r_{riskless} + \alpha (E[r_{risky}] - r_{riskless})$$

▶ Portfolio Standard Deviation $StDev_p = \alpha StDev_{risky}$

Playing with Algebra I

Rearranging the StDev formula above, we would get

$$\alpha = \frac{StDev_p}{StDev_{risky}}$$

Let's now substitute α in the Expected Return formula:

$$E[r_p] = r_{riskless} + \frac{StDev_p}{StDev_{risky}} (E[r_{risky}] - r_{riskless})$$

Or equivalently

$$E[r_p] = r_{riskless} + StDev_p \frac{(E[r_{risky}] - r_{riskless})}{StDev_{risky}}$$



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To Put It into



$$E[r_p] = r_{riskless} + StDev_p \frac{(E[r_{risky}] - r_{riskless})}{StDev_{risky}}$$

is the equation of as straight line drawn in the Risk-Expected Return plan, with slope

$$\frac{(E[r_{risky}] - r_{riskless})}{StDev_{risky}}$$

The ratio above technically goes under the name of **Sharpe Ratio**



The best achievable combination riskless asset/risky portfolio is the one that maximizes the Sharpe Ratio



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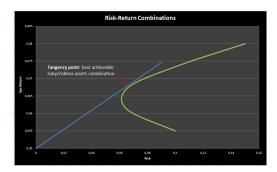
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A Graphical Approach



- Where would you represent the risk-free portfolio? Why?
- Investors will combine the tangency portfolio with the risk-free asset to form their overall portfolio: the allocation they choose depends on their preferences for risk

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- Depending on the proportions of your wealth that you decide to invest in the risky asset and in the riskless portfolio respectively, you will move along the straight line
- Assuming that α and (1α) represent the proportions of your wealth invested in the risky portfolio and in the risk-free asset respectively, which point on the line represents $\alpha = 0$?
- ▶ Which point on the line represents $\alpha = 1$?

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If T is the tangency portfolio, then $\forall i, j$

$$\frac{E[r_i]-r_f}{Cov(r_i;r_T)} = \frac{E[r_j]-r_f}{Cov(r_j;r_T)}$$

with i and j= securities belonging to T Remember that

$$Cov(z; Ax + By) = A \cdot Cov(z; x) + B \cdot Cov(z; y)$$

and assume T is made up of only two assets, so that

$$T = \omega r_i + (1 - \omega) r_j$$

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$$Cov(r_i; r_T) = \omega Cov(r_i; r_i) + (1 - \omega) Cov(r_i; r_j) = \omega Var(r_i) + (1 - \omega) Cov(r_i; r_j)$$

$$Cov(r_j; r_T) = \omega Cov(r_i; r_j) + (1 - \omega) Cov(r_j; r_j) = \omega Cov(r_i; r_j) + (1 - \omega) Var(r_j)$$

Let's substitue and solve for ω to determine the optimal (tangent) portfolio T to be best combined with the risk-free asset.

$$\frac{E[r_i] - r_f}{\omega Var(r_i) + (1 - \omega)Cov(r_i; r_j)} = \frac{E[r_j] - r_f}{\omega Cov(r_i; r_i) + (1 - \omega)Var(r_j)}$$



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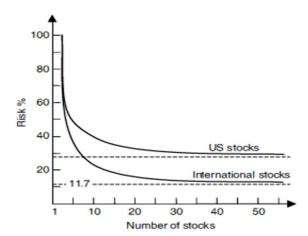
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- Rewards: Significant reduction in the volatility of the resulting portfolio
- ▶ **Risks**: An internationally-diversified portfolio is however subject to the risk of unexpected FX rate fluctuations

$$E[r_p] = r_{pF} + \Delta S_{\frac{F}{D}}$$

$$Var_p = Var(\Delta S_{\frac{F}{D}}) + Var(r_{pF}) + 2Cov(r_{pF}; \Delta S_{\frac{F}{S}})$$

- Var_{pF}: the variance of an internationally-diversified portfolio depends on...
- ▶ $Var(\Delta S_{\frac{F}{D}})$the variance of the FX rate...
- \blacktriangleright $Var(r_{pF})$:...the variance of the FC-denominated assets...
- ▶ $2Cov(r_{pF}; \Delta S_{\frac{F}{S}})$:...as well as on the **covariance** between them

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To Put It into

Home-Equity Bias

Even though it would be beneficial (for risk reduction) to diversify on an international scale, the global **holding of foreign securities is largely sub-optimal**





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- Legal barriers to foreign investments
- ▶ **Higher transaction costs** on foreign securities
- ► Indirect barriers to foreign investments (e.g. the difficulty in finding -and interpreting- information about foreign securities)
- Additional risks to be hedged (FX risk, country risk...)



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Го Put It into

- Investors are purely price-takers
- Investments are limited to a universe of publicly traded financial assets
- ▶ No taxes and no transaction costs
- Investors are rational mean-variance optimizers and have the same investment horizon
- Homogeneous expectations (same views) and risk appetite



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If all investors use identical mean-variance analysis. applied to the same universe of securities, for the same time horizon and use the same information set, they all must arrive at the same determination of the optimal risky portfolio on the efficient frontier...



...however, if all the investors hold an identical risky portfolio, this has to be the MARKET PORTFOLIO (including all tradable assets)

$$\frac{E[r_j]-r_f}{Cov(r_j;r_m)} = \frac{E[r_m]-r_f}{Var(r_m)}$$

with:

- ▶ $E[r_j]$: expected return on the j^{th} asset
- ▶ r_f: risk-free rate of return
- \triangleright $E[r_m]$: expected return on the market portfolio
- ▶ $Cov(r_j; r_m)$: covariance between asset j and the market portfolio
- \triangleright Var (r_m) : variance of the market portfolio

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$$r_{j} - r_{f} = \beta(r_{m} - r_{f})$$
$$\beta = \frac{Cov(r_{j}; r_{m})}{Var(r_{m})}$$

- $ightharpoonup r_i r_f$: The risk premium is linearly related to...
- ► $\frac{Cov(r_j;r_m)}{Var(r_m)}$:...the risk that the single asset contributes to the mkt as a whole \Rightarrow **SYSTEMATIC RISK**



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o Put It into

Investment where the investor's holding is too small to provide any effective control (Just to revise, could you define what a FDI is? Hint: step back to Lesson I...)



level of risk



Even common wisdom suggests that putting all eggs in one basket can be very risky!



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- Asset-Specific Risk = Non-Systematic Risk =
 Diversifiable Risk: risk that can be diversified away.
- Mkt Risk = Systematic Risk = Non Diversifiable Risk: risk that remains even after extensive diversification



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- Systematic risk: risk that cannot be diversified away
- Systemic risk: risk of collapse of an entire financial system or entire market



Efficient Frontier

Optimal set of portfolios that offer the highest expected return for a specific level of risk (Markowitz, 1952)



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Riskless assets

Financial instruments that have a **certain** future return (MM securities, Government bonds...)

 $\downarrow \downarrow$

Are they truly (and completely) riskless in practice?



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To Put It into

Sharpe Ratio: measure for calculating risk-adjusted returns. In more quantitative terms, it can be defined as the average return earned in excess of the risk-free rate per unit of volatility



- Integrated Capital Markets: the connection among international capital markets is seamless
- Segmented Capital Markets: implicit or explicit factors inhibit the free movement of capital among the various countries

WATCH OUT: HEB is the most obvious example of capital market segmentation



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▶ Portfolio 1

Constituents	Weight	E(r)	Var(r)	Cov(a,b)
Stock a	0.6	0.15	0.19	0.4
Stock b	0.4	0.07	0.25	

▶ Portfolio 2

Constituents	Weight	E(r)	Var(r)	Cov(c,d)
Stock c	0.3	0.1	0.23	0.3
Stock d	0.7	0.15	0.12	



- ▶ 10.2 Suppose that the risk premium on the market portfolio is estimated at 0.08 with a standard deviation of 0.22. What is the risk premium on a portfolio invested 0.25 in Apple and 0.75 in Google, if they have β = 1.10 and 1.25, respectively?
- ▶ 10.3 Stock ABC has an expected return of 0.12 and β = 1. Stock XYZ has expected return of 0.13 and β = 1.5. The market's expected return is 0.11 and r_f = 0.05. According to the CAPM, which stock is a better buy? Why?



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▶ Portfolio 1

Constituents	Weight	E(r)	StDev(r)
Stock a	0.3	0.14	0.2
Stock b	0.3	0.08	0.12
Stock c	0.3	0.02	0.3

▶ Portfolio 2

Constituents	Weight	E(r)	StDev(r)
Stock d	0.3	0.2	0.28
Stock e	0.3	0.18	0.33
Stock f	0.3	0.33	0.4

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▶ Portfolio 1

Correlations	a	b	С
a	1	0.5	0.2
b	0.5	1	0.4
С	0.2	0.4	1

► Portfolio 2

Correlations	d	е	f
d	1	0.3694	0.1539
е	0.3694	1	0.2148
f	0.1539	0.2148	1



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