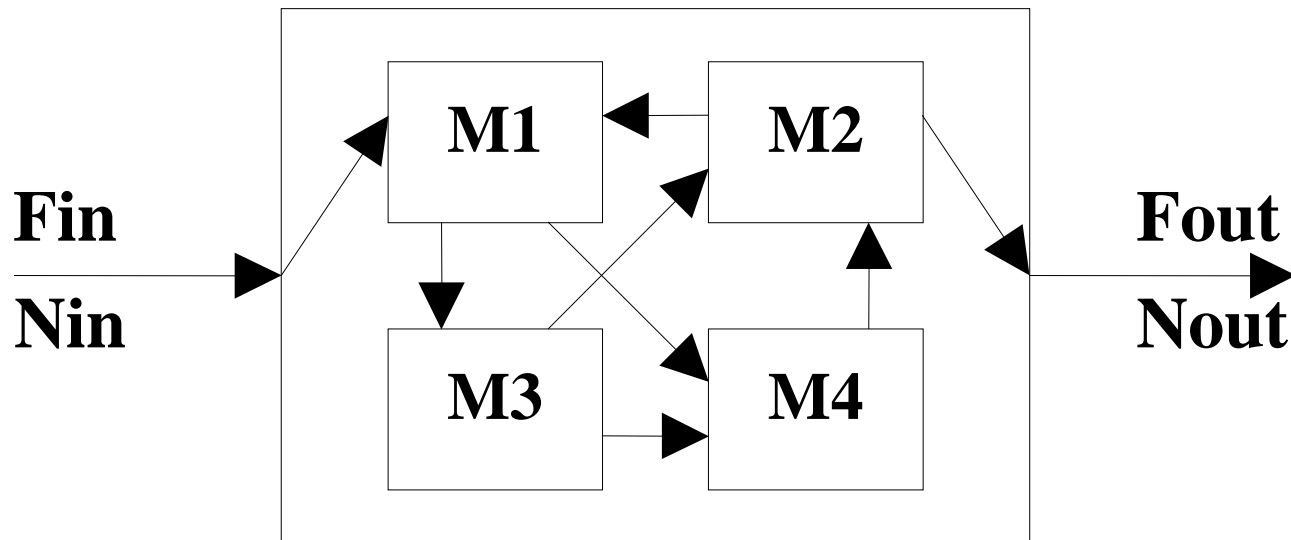




Throughput diagrams

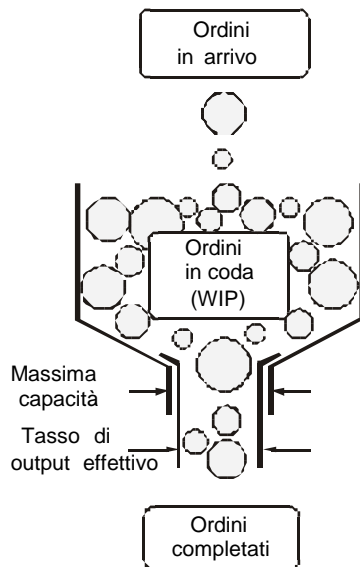
Given a production system

- F_{in} , F_{out} input/output frequency (rate) (pcs/d)
- N_{in} , N_{out} input/output number of pieces starting from $t = 0$ (pcs)

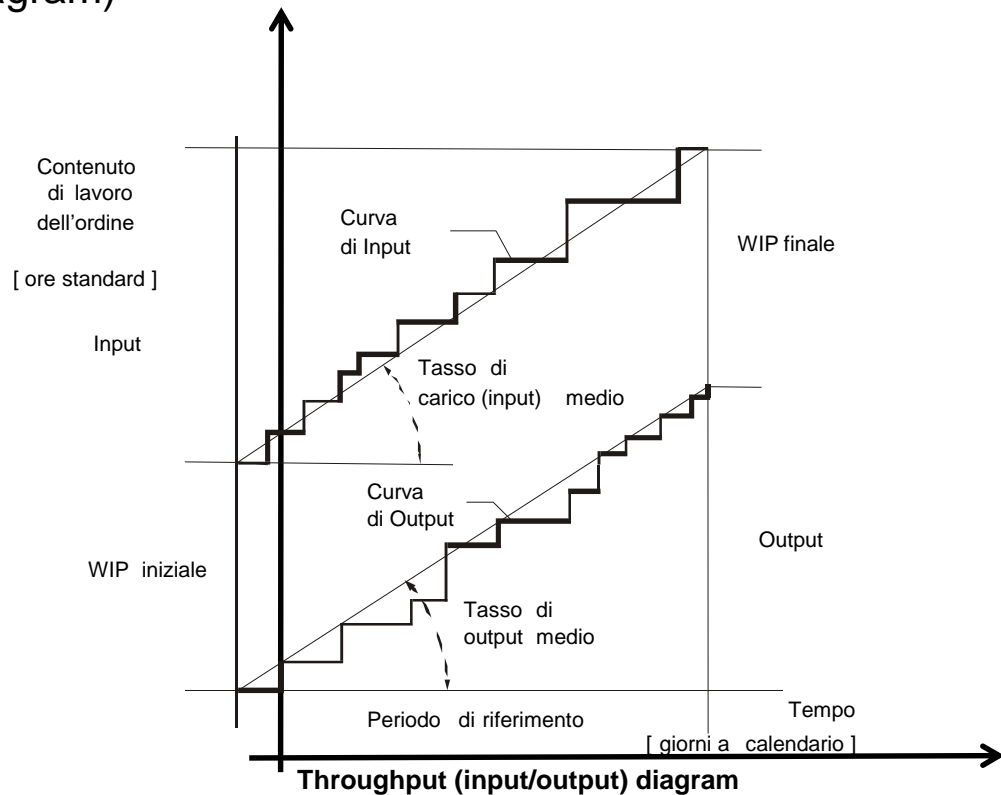


Funnel Model

The *throughput* diagram is a model used to monitor the process in the *funnel* (production system) \Rightarrow starting from the funnel events (arrivals, exit) it is possible to build up a *throughput* diagram per area (input/output diagram)



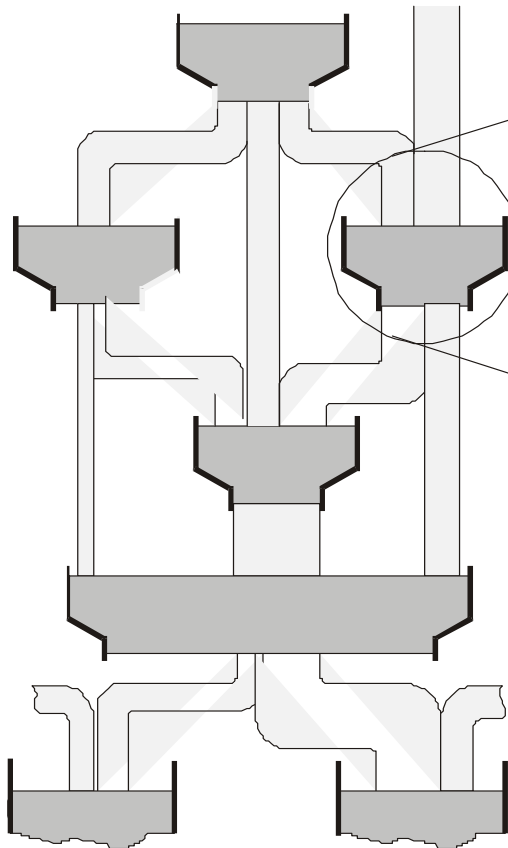
Funnel model



Throughput (input/output) diagram

Funnel Model

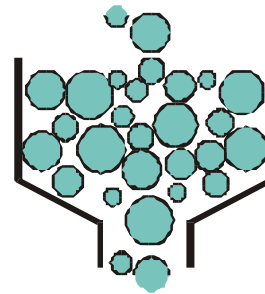
FLUSSO DEI MATERIALI



Funnel Model

Ordini in Arrivo

(il funnel è “destinazione” dei flussi)



Ordini Completati

(il funnel è “origine” dei flussi)

Input/output diagram

- Hp: production system with steady load ($F_{in} = \text{constant}$)
- On that condition, the trend of number of parts in input N_{in} is linear
 - If the bottleneck is not saturated ($F_{in} < TH_{max}$), the number of pieces in output from the system N_{out} will have the same trend shifted to the right.

Input/output diagram

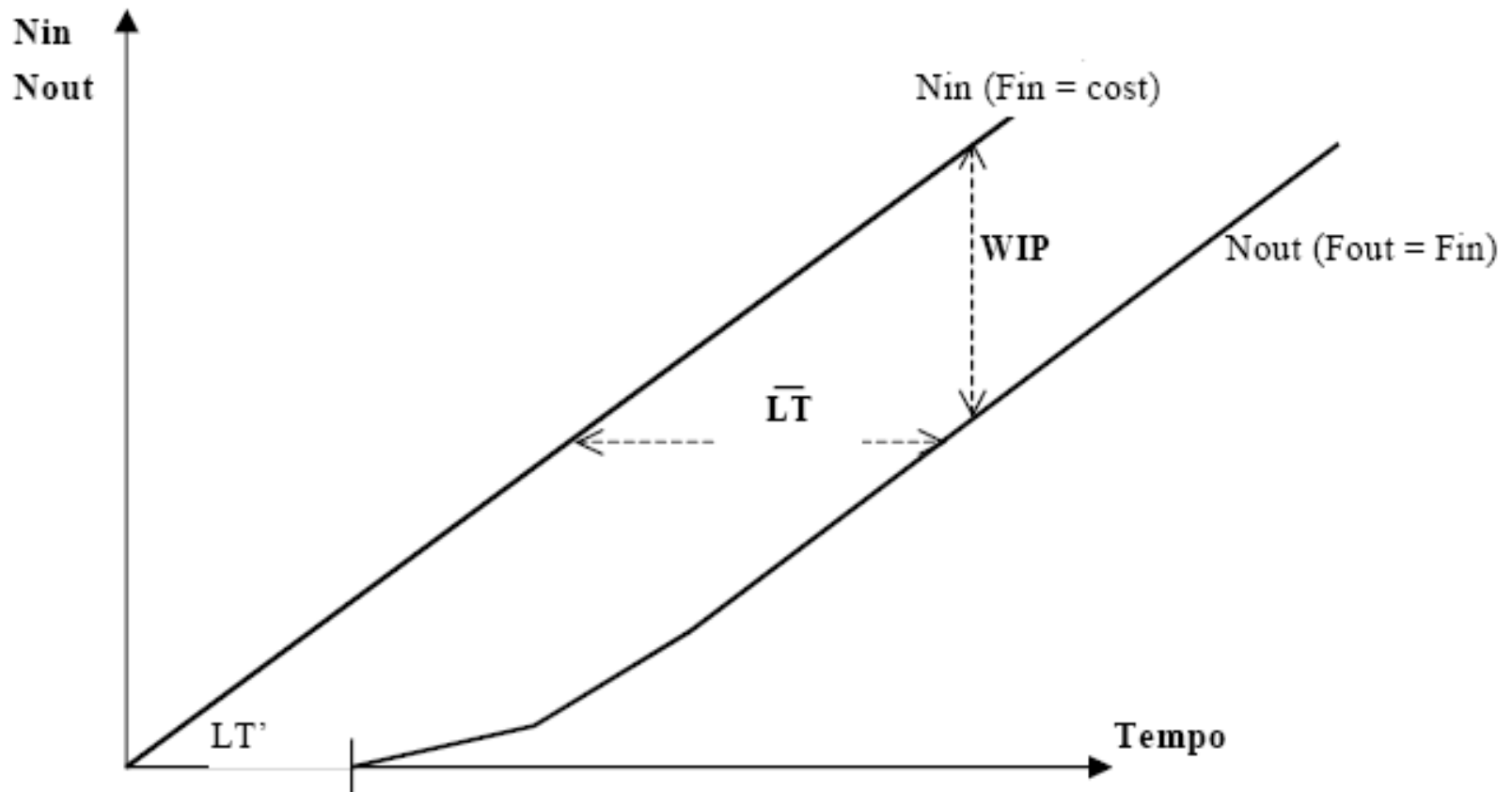
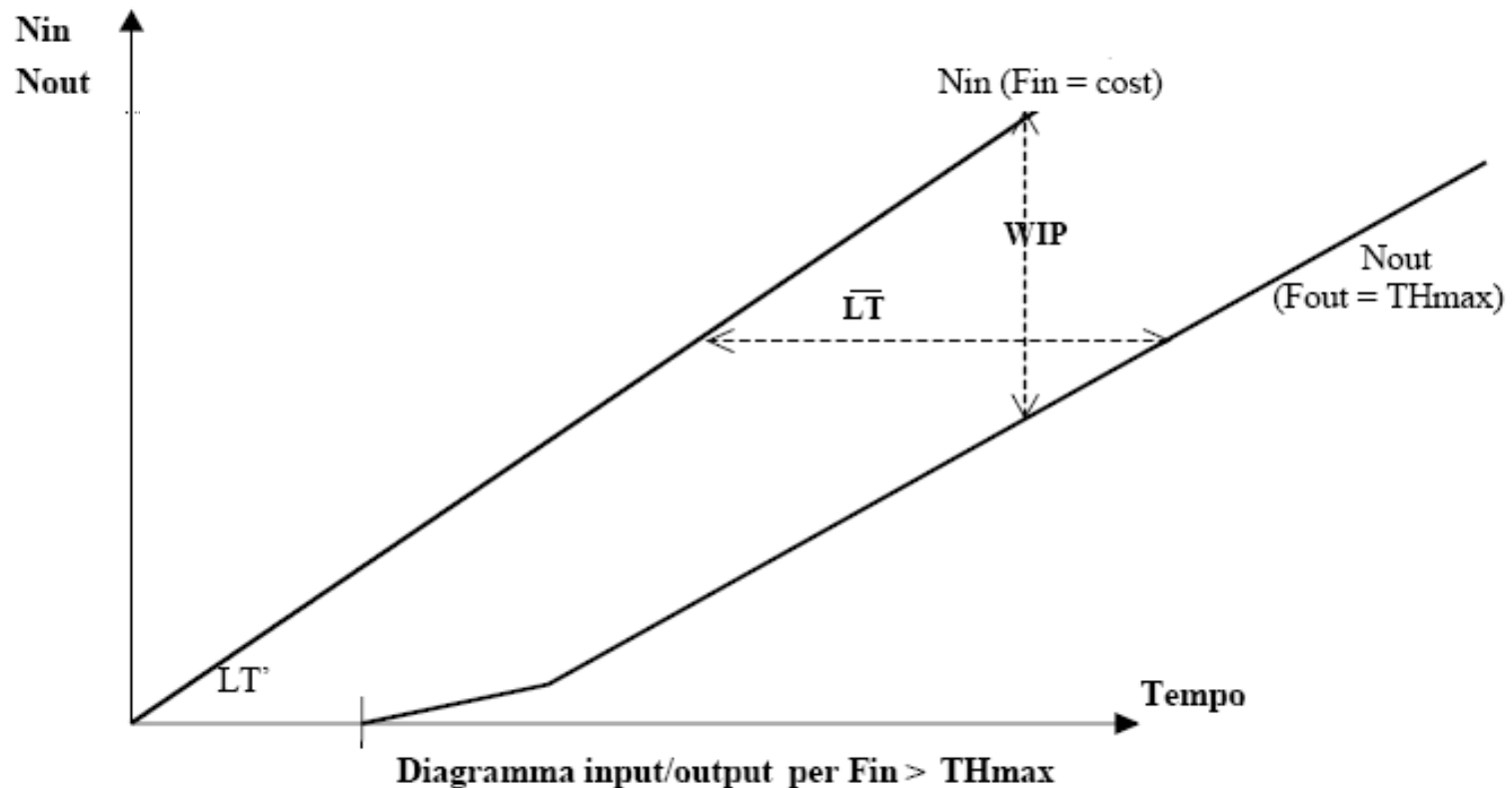


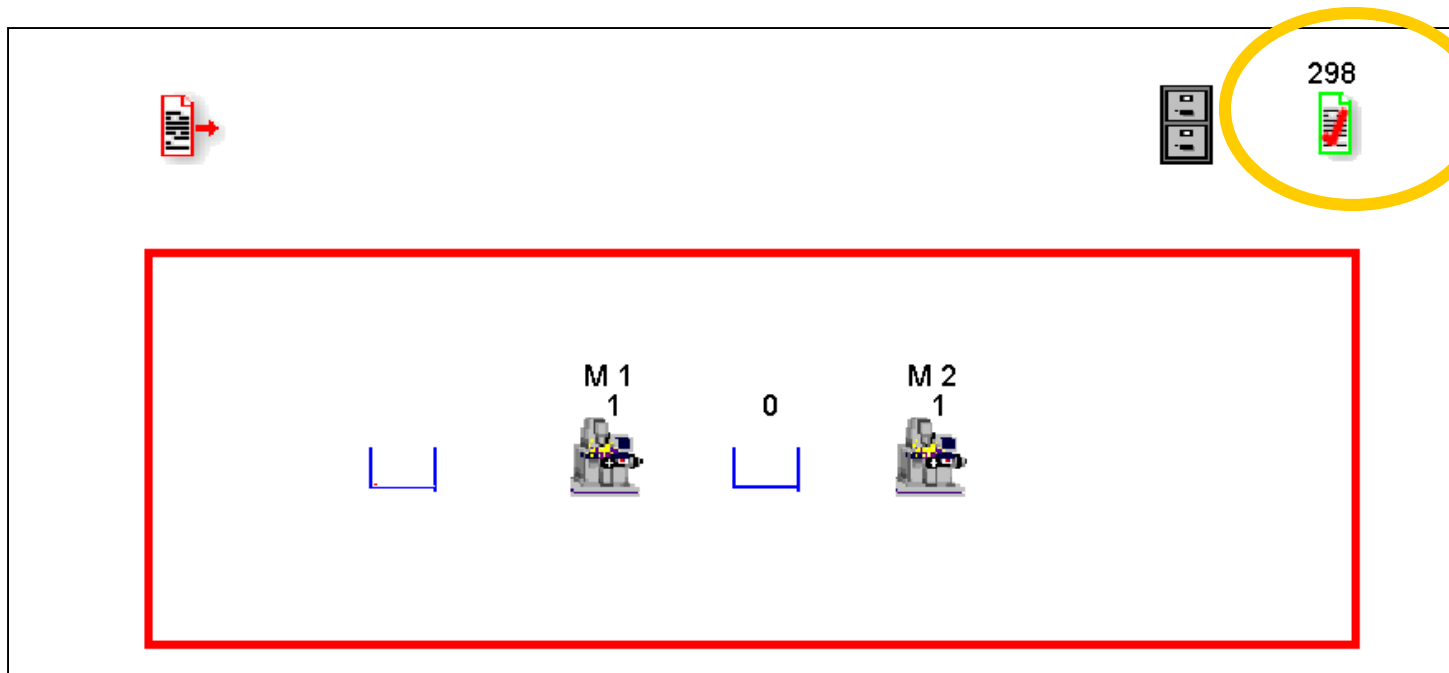
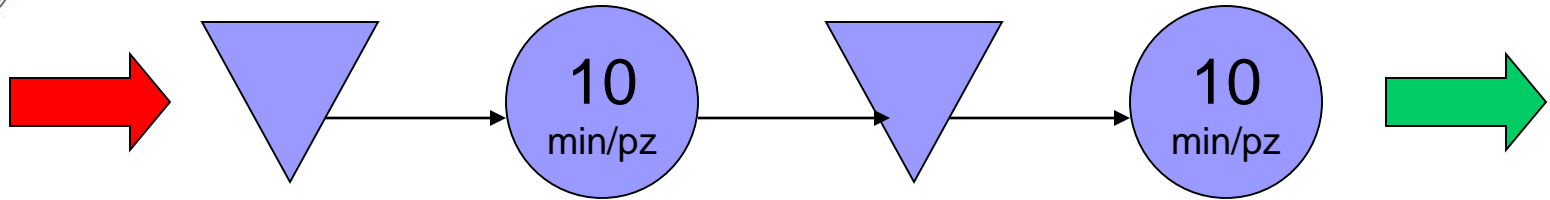
Diagramma input/output per $F_{in} < TH_{max}$

Input/output diagram

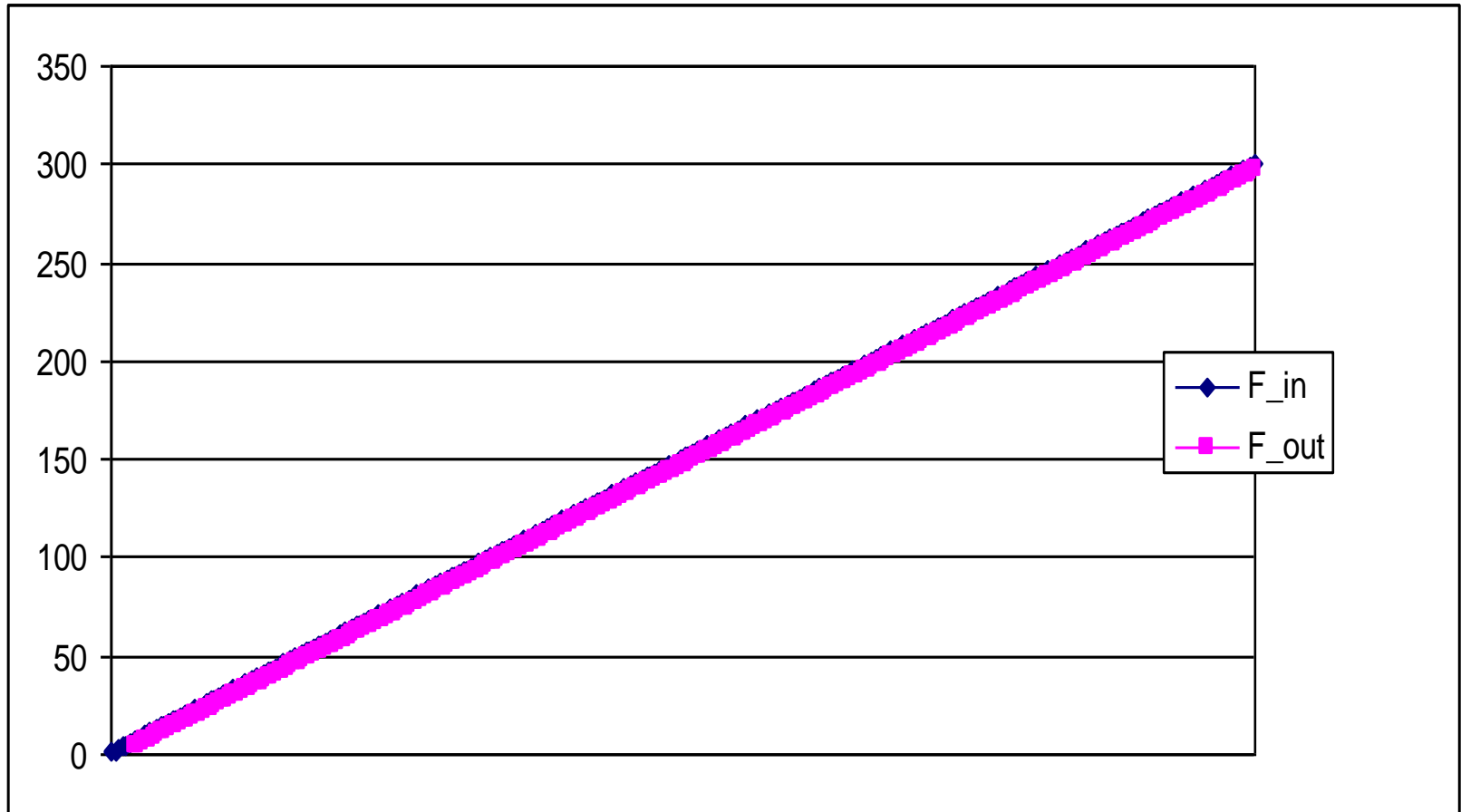
- When F_{in} is over TH_{max} (TH_{cb}), the number of parts in input cannot be worked and, for that reason, WIP and LT will increase



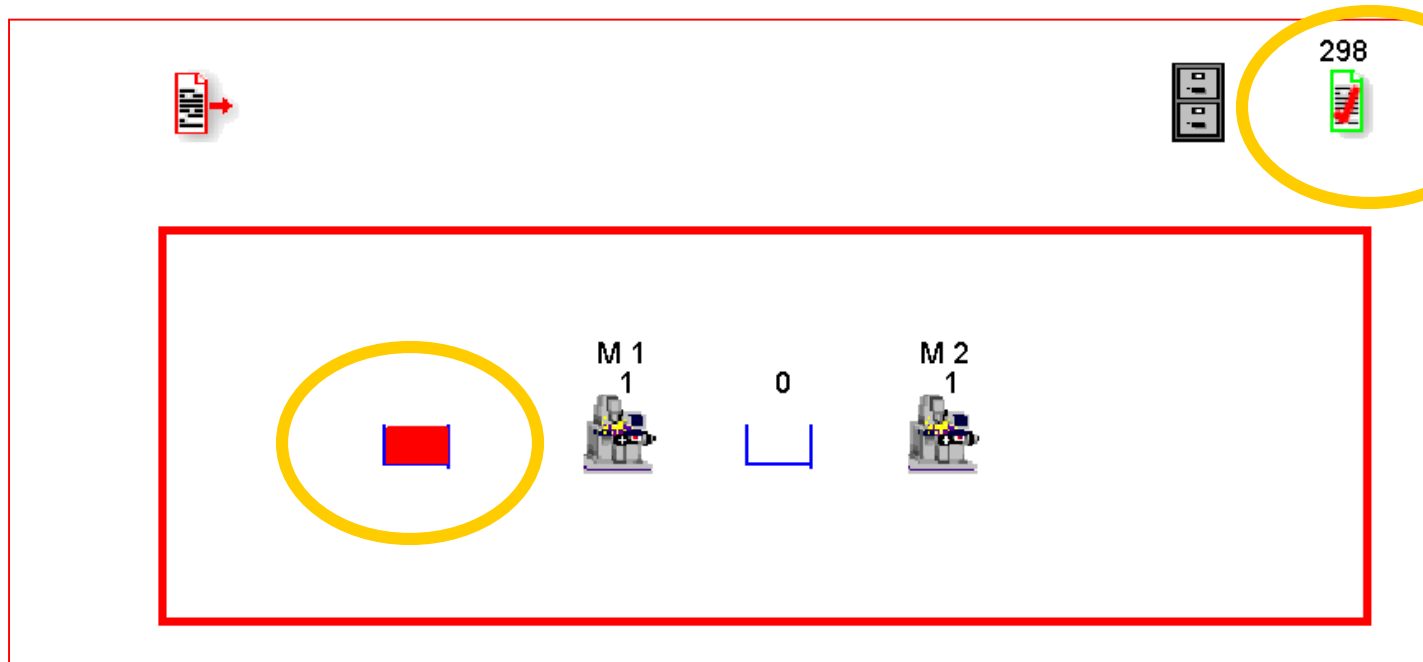
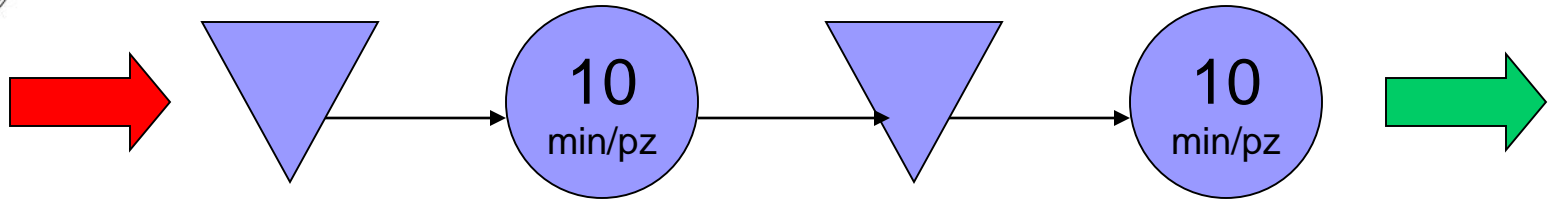
Input/output diagram



Input/output diagram



Input/output diagram



Input/output diagram

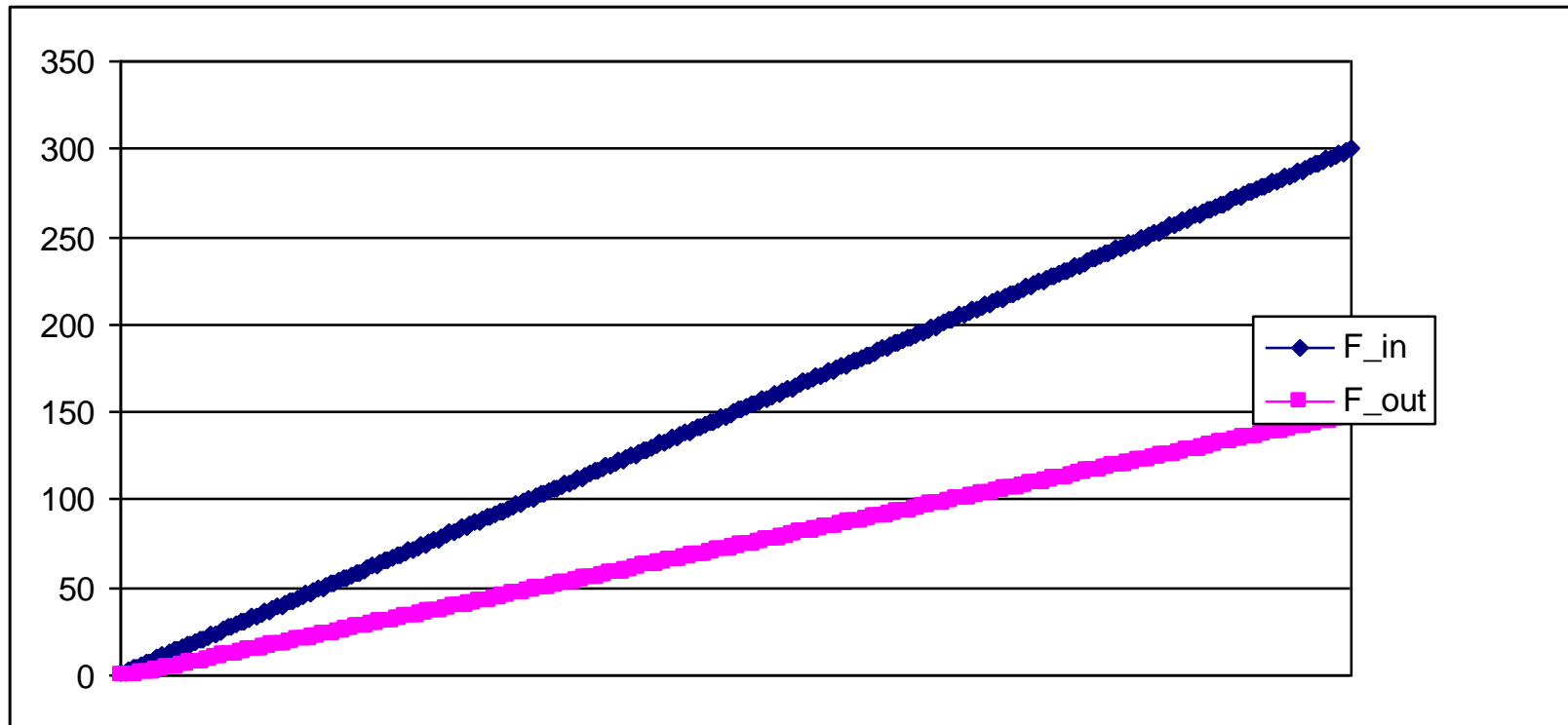


Diagram in a real situation

Data collection from production data feedback registry

Order number	Work content TO [hour/order]	Data input [calendar day]	Data output [calendar day]
1	20	98	100
2	21	94	102
3	19	101	103
4	23	101	105
5	11	102	106

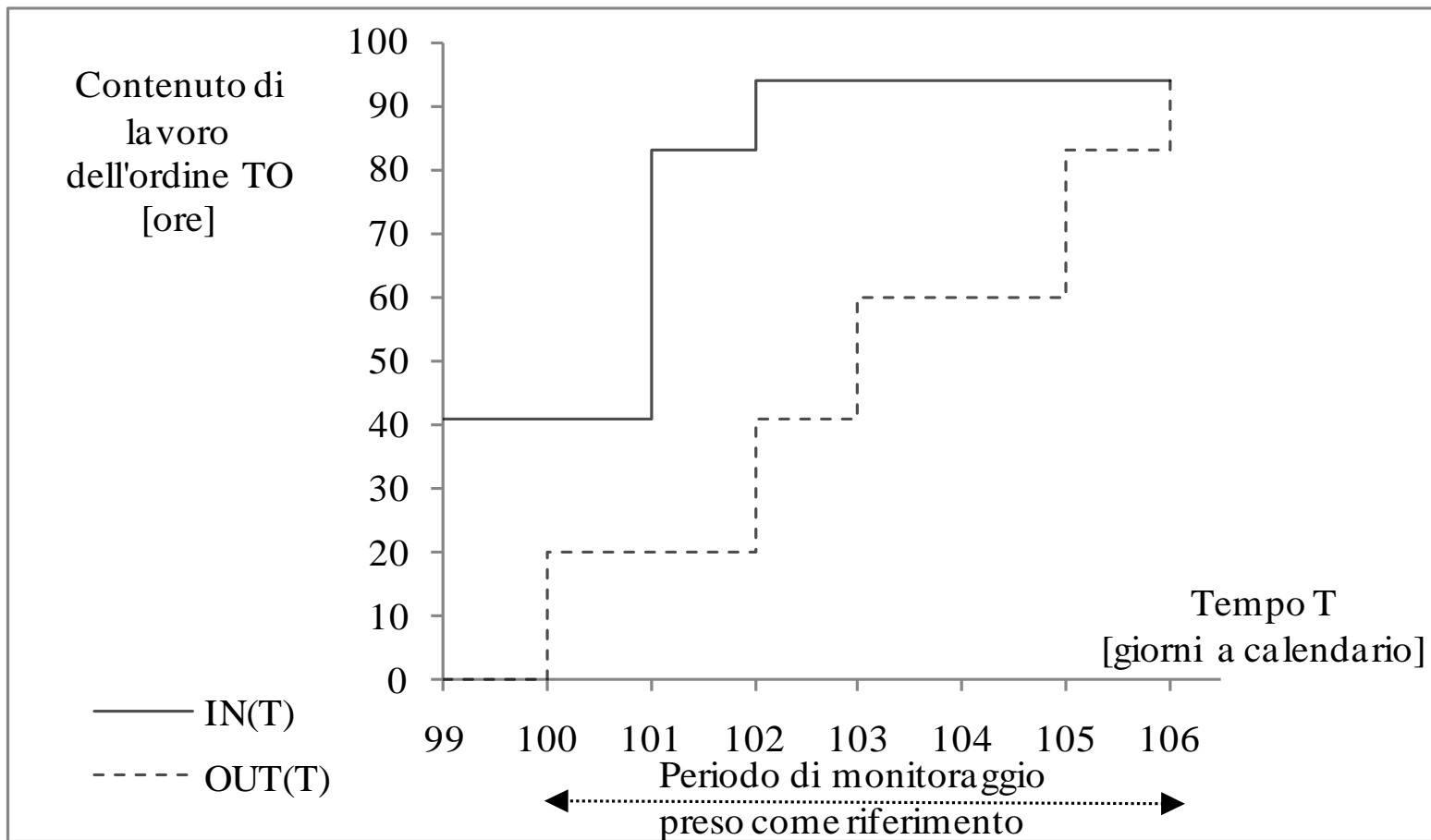
Work content of the orders

- Order work content (TO) is the sum of set up time and work time (or processing time) of the parts within a production batch

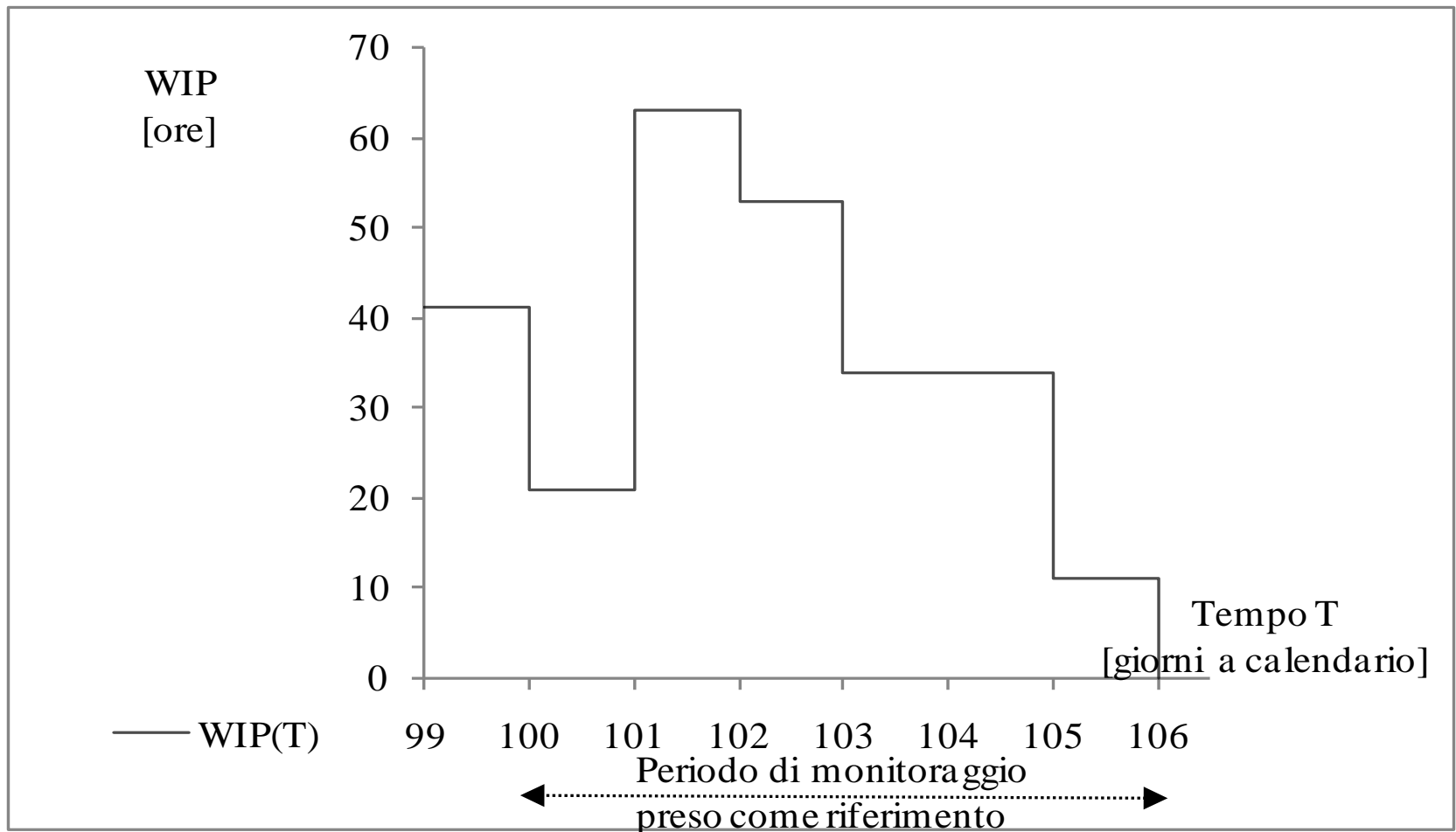
$$TO = \frac{TS + LS \times TP}{60}$$

- Where
 - TO work content of the order [hour / order]
 - TS standard setup time [min / order]
 - LS standard batch dimension [# parts / order]
 - TP standard processing time of a single piece [min / part]

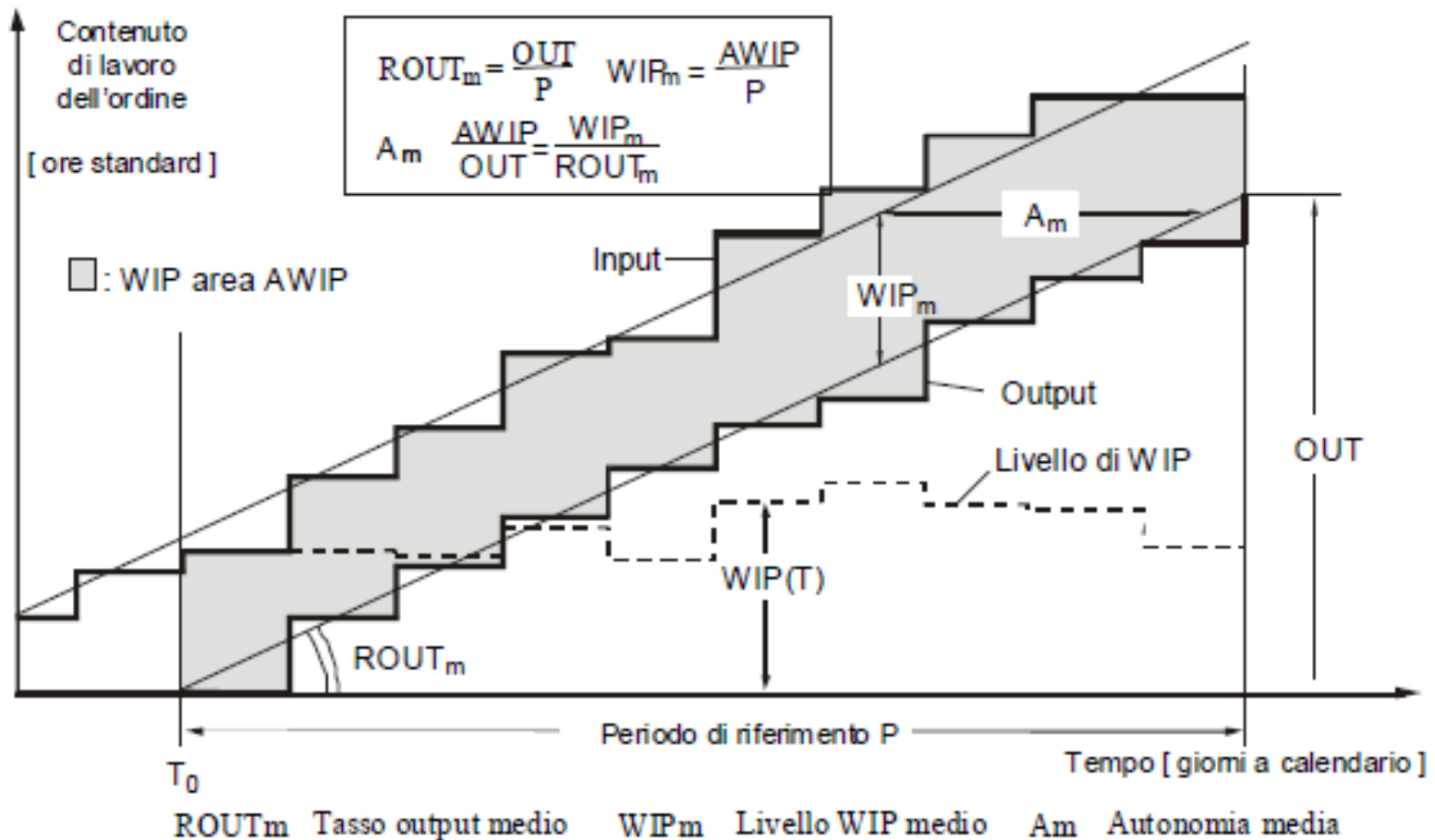
Input/output curves



WIP level curve



Performance indicators



Performance indicators

- Vertical distance

$$WIP(T) = IN(T) - OUT(T)$$

- $WIP(T)$ WIP level at time T
- $IN(T)$ Sum of work content orders arrived in the system before time T
- $OUT(T)$ Sum of work content orders completed by the system before time T

Performance indicators

- Mean vertical distance

$$WIP_m = \frac{\int_{T_0}^{T_1} IN(T) \times dt - \int_{T_0}^{T_1} OUT(T) \times dt}{T_1 - T_0}$$

- WIPm Mean level of WIP [hour]
- T0 start of monitoring period [SCD – Stock Calendar Days]
- T1 end of monitoring period [SCD]

Performance indicators

- Mean rate of Output curve (ROUTm)
 - ROUTm mean output rate [SCD]
 - TOj work content of order j [hour/order]
 - nout number of orders completed within monitoring period
 - P length of monitoring period [SCD]

$$ROUT_m = \frac{\sum_{j=1}^{n_{out}} TO_j}{P}$$

- RINm rate is defined in the same way, using the number of incoming orders nin within monitoring period

Performance indicators

- The higher RIN_m , the greater the number of hours requested, in terms of production capacity, from the orders in input within the monitoring period
- The higher $ROUT_m$, the greater the available production capacity to complete the orders arrived within monitoring period
- A stable system has $ROUT_m \cong RIN_m$

Performance indicators

- Mean horizontal distance

- Operative autonomy A_m is a measure of the time (calendar time) after which, in absence of incoming orders, the station becomes empty

$$A_m = \frac{WIP_m}{ROUT_m}$$

- A_m Mean operative autonomy [SCD]
- WIP_m Mean level of WIP [hours]
- $ROUT_m$ Mean output rate [hours / SCD]

Performance indicators

- Mean use of production capacity measures how much production capacity ($ROUT_m$) is used given the maximum production capacity ($ROUT_{max}$)

$$UT_m = \frac{ROUT_m}{ROUT_{max}} \times 100$$

- UT_m Mean use of production capacity
 - $ROUT_{max}$ = Maximum (standard) production capacity available in a station
- UT_m measures the percentage of inefficiencies (leaks) related to internal and external causes
- $1-UT_m$ is the mean leak

Use of diagram

- The analysis of throughput diagram helps to check the existence of production capacity leaks.
- This leaks can be caused by:
 - “Internal” causes
 - “External” causes

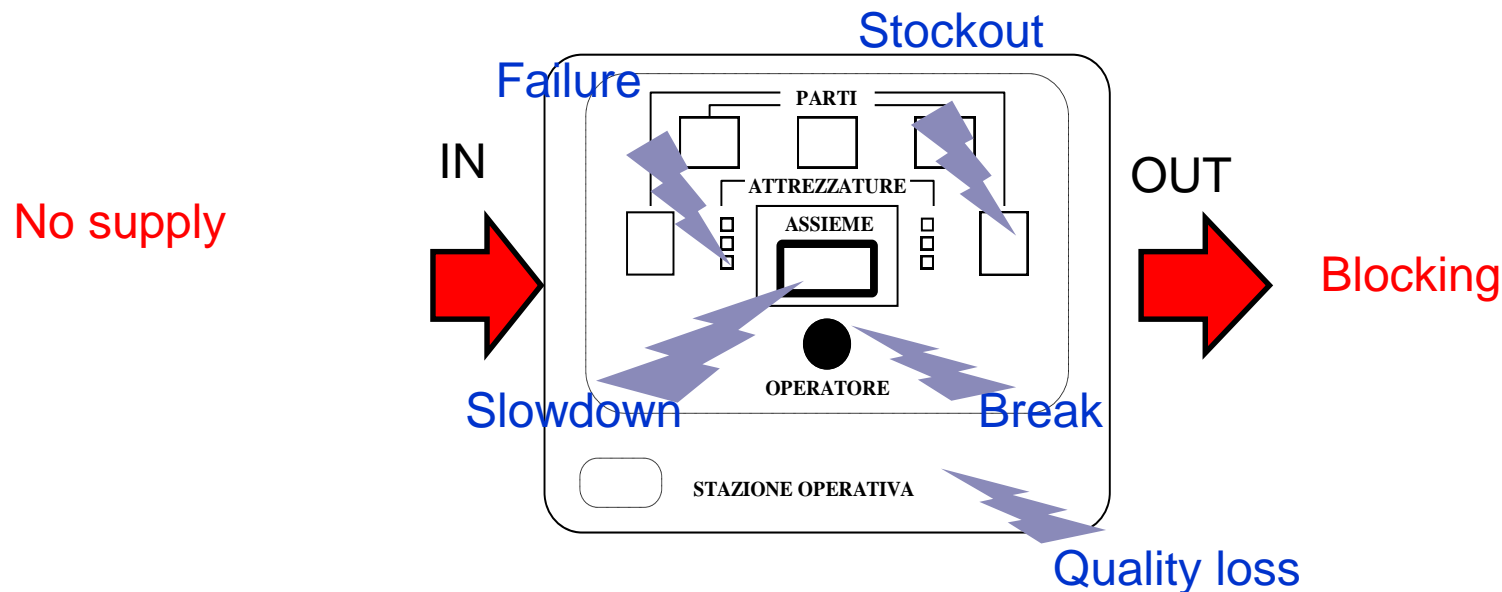


Diagram uses

- Leaks are characterized by
 - **Causes:** Events within production area (es. failures, breaks, operators unavailability)
 - **Symptoms:** Decrease of $ROUT_m$ without RIN_m reduction
- “Internal” leaks can depend on performances of external support processes
 - E.g. no supply
 - Symptom: reduction of RIN_m
 - E.g. the next station/area does not consume correctly the material produced by this station/area and, for that reason, the interoperational buffer is filled (blocking)
 - Symptom: reduction of $ROUT_m$

Diagram uses

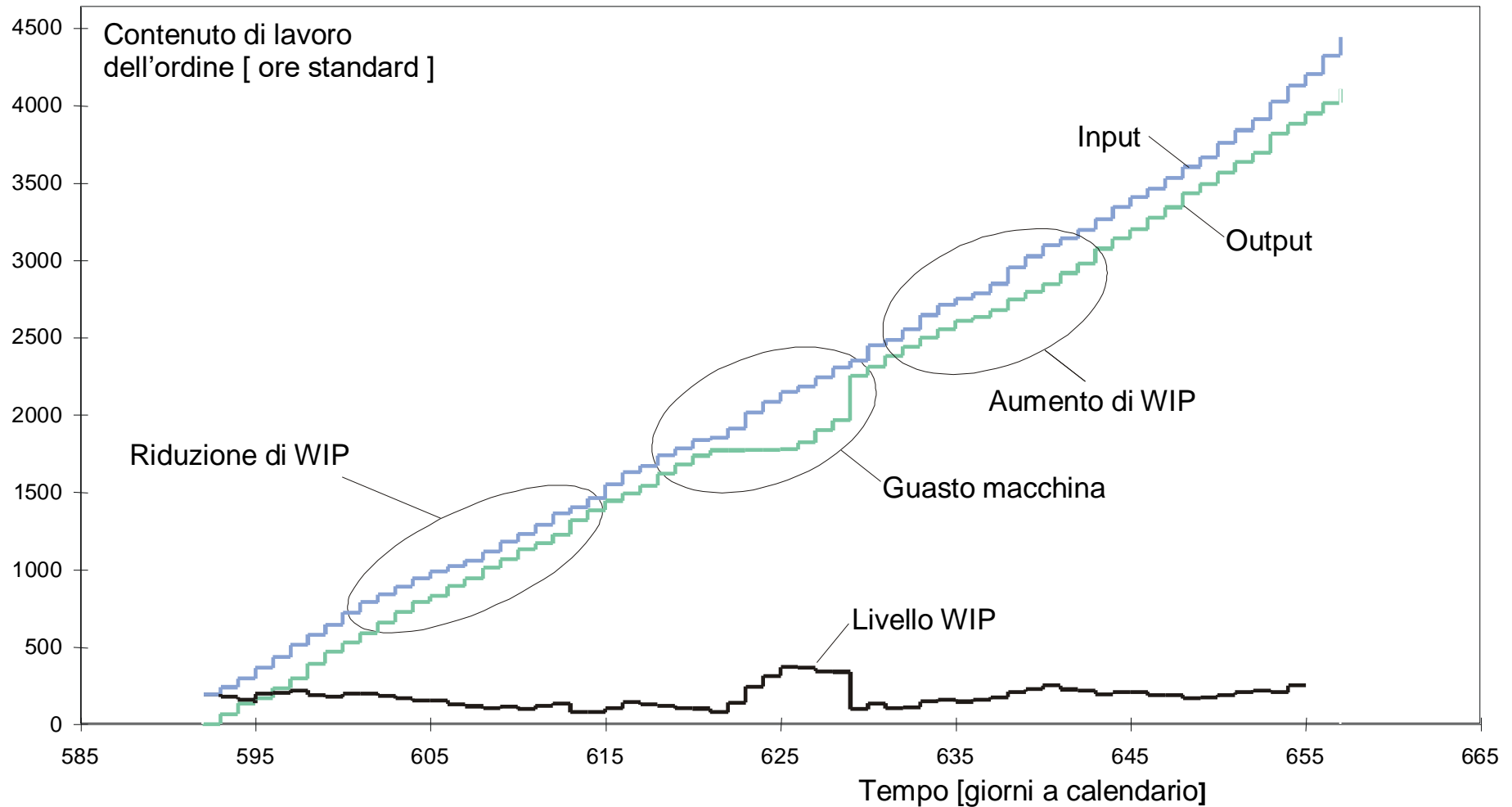
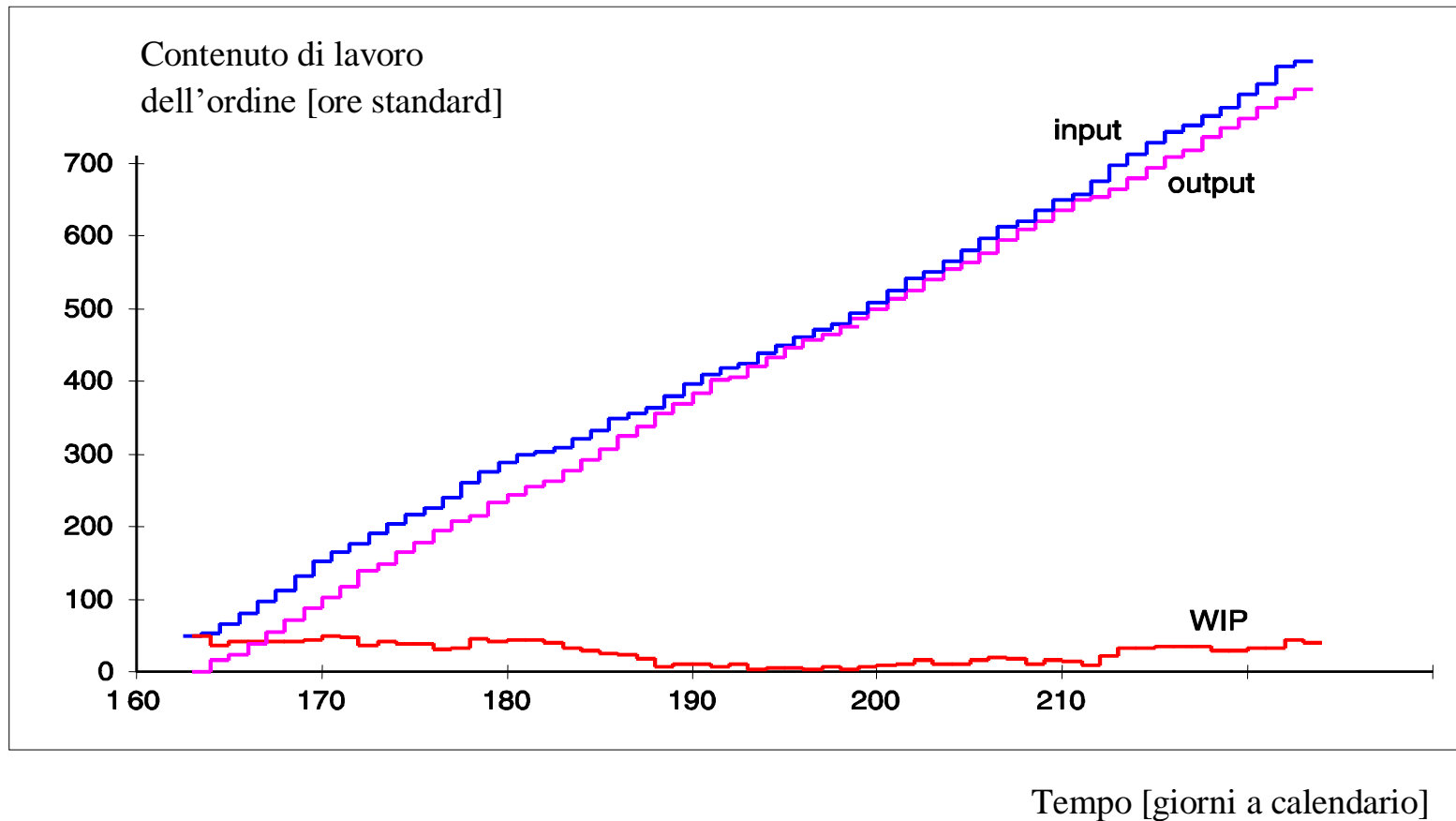
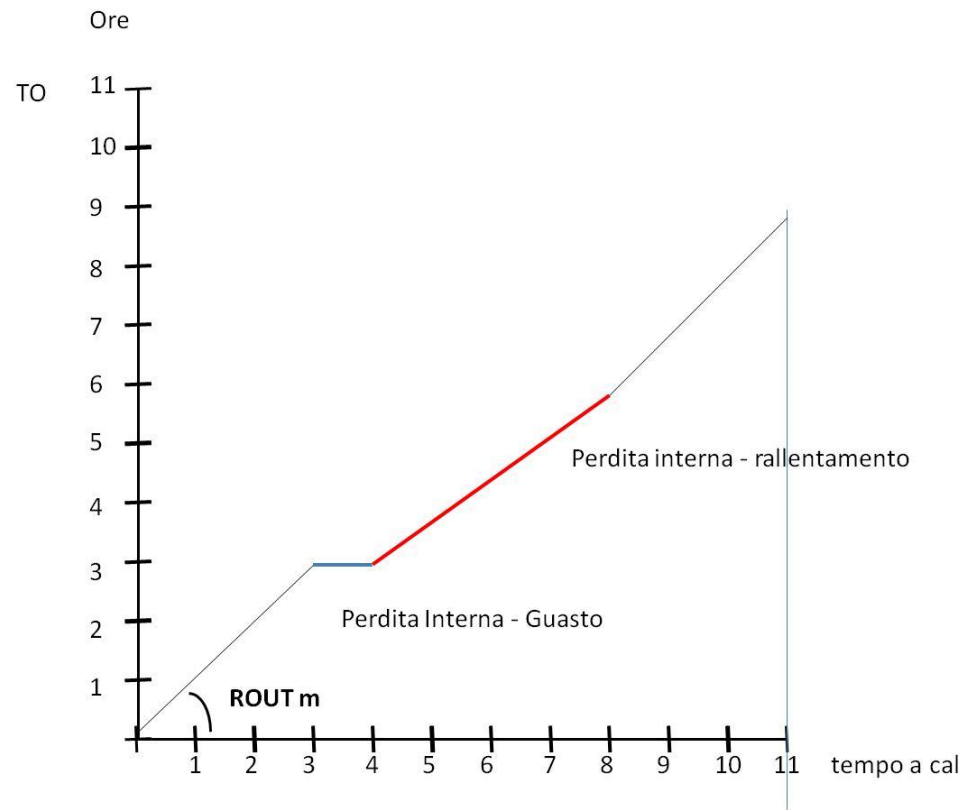
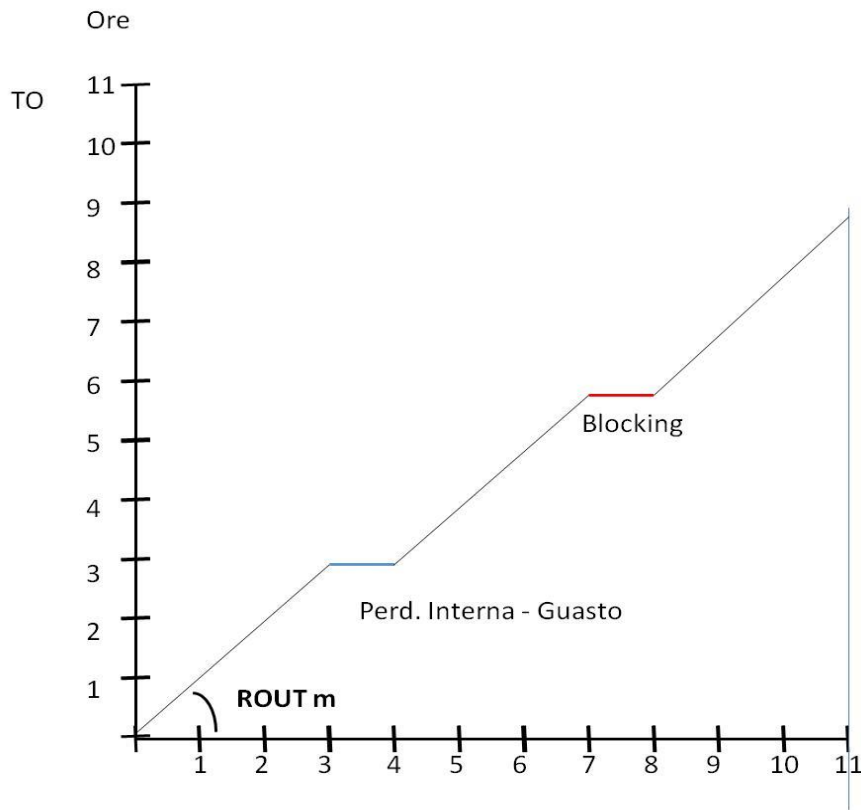


Diagram uses



Uses of diagram



Uses of diagram

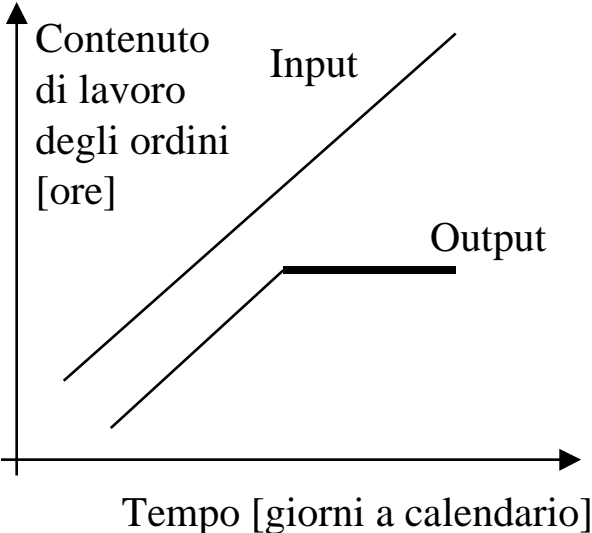
Input / output curves	Causes
 <p>The graph plots 'Contenuto di lavoro degli ordini [ore]' on the vertical axis against 'Tempo [giorni a calendario]' on the horizontal axis. Two lines are shown: 'Input', which is a straight line starting from the origin and increasing linearly; and 'Output', which follows the 'Input' line until it reaches a certain point, then becomes a horizontal line, indicating that the output has stopped increasing despite the input continuing to rise.</p>	<p>Internal leaks (e.g. failures, unavailability of auxiliary resources, etc.) or external (blocking)</p>

Diagram uses

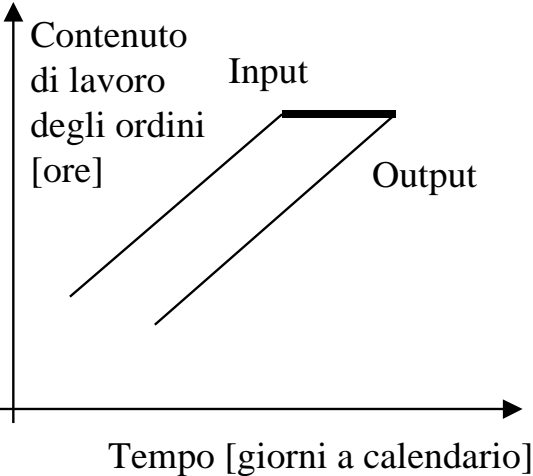
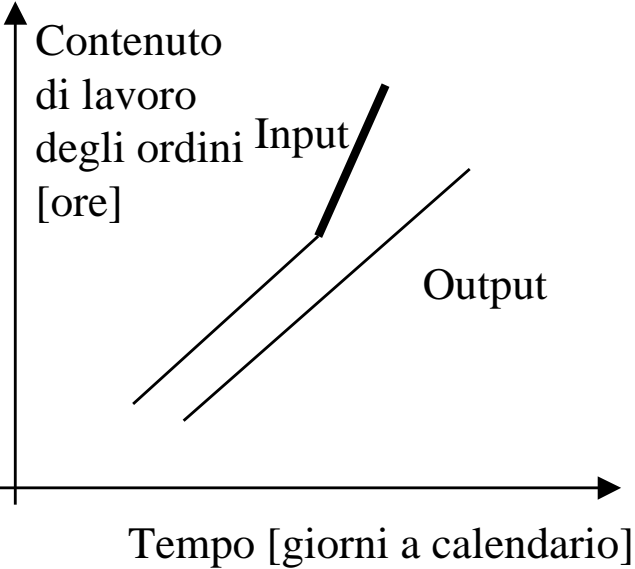
Input / output curves	Causes
 <p>The graph illustrates the relationship between work content and time for input and output. The vertical axis represents the work content of orders in hours, and the horizontal axis represents time in calendar days. The 'Input' curve shows a linear increase in work content over time, which then levels off. The 'Output' curve shows a similar linear increase but is delayed and lower in magnitude, indicating a bottleneck or 'no supply' situation.</p>	<p>External leaks in a previous area, that lead to a 'no supply' situation</p>

Diagram uses

Input / output curves	Causes
 <p>Contenuto di lavoro degli ordini [ore]</p> <p>Input</p> <p>Output</p> <p>Tempo [giorni a calendario]</p>	<p>The available capacity cannot be increased in order to follow the requested capacity : increasing of R_{in} without a correspondent increasing of R_{out} (the available capacity is already fully used)</p>